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THESIS

EXPERIMENTAL DETERMINATION OF
THE ISOTHERMAL TEMPERATURE
COEFFICIENTS OF REACTIVITY AND
TEMPERATURE DEPENDENT THERMAL
DISADVANTAGE FACTORS OF THE
CORNELL UNIVERSITY ZERO
POWER REACTOR

WALTER PIERSON WYNN, JR.

1965

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EXPERIMENTAL DETERMINATION OF THE ISOTHERMAL TEMPERATURE COEFFICIENTS OF REACTIVITY

AND

TEMPERATURE DEPENDENT THERMAL DISADVANTAGE FACTORS
OF THE

CORNELL UNIVERSITY ZERO POWER REACTOR

A Thesis

Presented to the Faculty of the Graduate School
of Cornell University for the Degree of
Doctor of Philosophy

bу

Walter Pierson Wynn, Jr.

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BIOGRAPHY

The author was born in Gainesville, Florida, on 30 March, 1937. He received a competitive appointment to attend the United States Naval Academy from Congressman D. R. Matthews. In June, 1959, he was graduated with distinction from the U. S. Naval Academy, awarded the degree Bachelor of Science, and commissioned an Ensign in the U. S. Navy.

For the next thirteen months, the author was on sea duty onboard the conventionally powered submarines USS TROUT (SS 566), and USS CORPORAL (SS 346). On being designated "qualified in submarines" in August, 1960, he was detached from submarine duty and was ordered to report to the Commanding Officer, U. S. Naval Reserve Officer Training Corps Unit, Cornell University, for duty under instruction under the provisions of the Junior Line Officers Advanced Scientific Education Program. The JLOASEP program is also called the Burke Program in honor of Admiral Arleigh A. Burke who initiated the program while he was Chief of Naval Operations.

The author is a member of the U. S. Naval Institute, and a student member of the American Nuclear Society.

NOTICE

Lieutenant W. P. Wynn, Jr., U. S. Navy, attended Cornell University under the provisions of the Junior Line Officers Advanced Scientific Educational Program which is sponsored by the U. S. Navy Bureau of Personnel and the U. S. Naval Postgraduate School, Monterey, California.

This thesis is dedicated to the memory of the officers and men who lost their lives on the USS THRESHER (SSN-593) on 10 April, 1963.

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Lt. Charles R. MacVean, U.S.N., calculated temperature dependent thermal parameters for his own thesis, and it was these calculations which suggested the temperature dependent study of the disadvantage factor. Many discussions with him were of great value, and he also assisted by providing computer operator time.

Professor K. B. Cady provided many useful ideas and suggestions and in addition, he was available on a moment's notice for discussions.

Several graduate students contributed to the data reduction by providing computer codes or computer operator time. William E. Schilling has written or rewritten many data reduction codes for use with the Control Data Corporation 1604 computer installed in the Cornell Computing Center. In addition, he provided computer operator time and invaluable advice. David J. Osias developed the program for calculating

the temperature coefficient of reactivity. Donald H. Bryce and William E. Schilling worked together on the program RHOFIT, without which the accuracy and efficiency of the temperature coefficient experiments would have suffered. Thanks are due to the Cornell Computing Center, for without free machine time, the foregoing acknowledgments would not have been necessary.

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The author wishes to thank the many people who influenced him and made possible his selection for the Junior Line Officers Advanced Scientific Education Program.

The author would also like to thank the Commanding Officers and the staff of the N.R.O.T.C. Unit, Cornell University for the administrative aid received. In addition, he wishes to express particular gratitude to Mrs. C. M. Gumz of the Bureau of Naval Personnel for her cheerful assistance in administrative matters.

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CHAPTER 1

INTRODUCTION

1.1 GENERAL

One of the most important characteristics of a nuclear reactor is the effect of temperature on reactivity. As the temperature of the moderator, fuel, or reflector are individually changed, the effect on the reactivity may be quite different. Because it is difficult to mock up a temperature profile in a low power reactor, it is common to discuss temperature effects in terms of the isothermal temperature coefficient of reactivity where isothermal implies that all parts of the reactor are at a constant and uniform temperature. Comparison of the measured and calculated isothermal temperature coefficient aids progress toward understanding the physical processes taking place in the reactor.

This dissertation is concerned with two aspects of thermal effects on reactivity. The first is an experimental study of the isothermal temperature coefficient of reactivity of the Cornell University Zero Power Reactor, a light-water moderated, 2.1% enriched, UO $_2$ fueled, aluminum clad reactor having nominal water-to-fuel ratios of 1:1, 1.5:1, 2:1, 3:1, and $4:1.\frac{1}{2}$ (See Appendix A for fuel and lattice parameters.)

^{1/} S. S. Berg, "Initial Experiments on the Cornell University Zero Power Reactor Cores," CURL-7, p. 220 Cornell University Reactor Laboratory (1964).

Sec. 1.1 - 1.2

A theoretical prediction is given in Chapter 2, and the experimental techniques and results are discussed in Chapter 3.

The second aspect of this work singled out the temperature dependence of the disadvantage factor as one contribution to the temperature dependent behavior of the reactor. Chapter 4 discusses the theoretical basis of the use of foils to measure disadvantage factors. Experimental methods and results are discussed in Chapter 5 and compared with predictions by MacVean $\frac{2}{}$

Chapter 6 summarizes the results of both aspects of this work and suggests further experimental studies.

1.2 ISOTHERMAL TEMPERATURE COEFFICIENT OF REACTIVITY

The isothermal temperature coefficient α is defined as $d\rho/d\theta$ where ρ is excess reactivity and θ is the temperature of all parts of the core. Isothermal coefficients of reactivity have previously been measured for cores similar to the Cornell critical assembly. In these studies, temperature dependent excess reactivities were determined either by measuring periods for a given control rod configuration or by measuring the change in critical position for a calibrated control rod.

^{2/} C. R. MacVean, "A Simplified Cell Theory Applied to the Calculation of Thermal Neutron Spectra in Light Water Lattices," CURL-10, p. 145 Cornell University Reactor Laboratory (1964).

The Westinghouse temperature coefficient experiments $\frac{3,4}{}$ were made on aluminum clad, 1.3% enriched metal and oxide fuels of both 0.600 and 0.387-inch diameters. Reactivity values were determined by measurement of periods longer than 100 seconds. Water-to-fuel ratios from 1.5:1 to 5:1 were studied over a temperature range of 20-50°C.

The Yankee cores, also studied by Westinghouse, $\frac{5}{}$ had 2.2:1 and 2.9:1 water-to-fuel ratios for 2.7% enriched, stainless steel clad, 0.300-inch diameter UO₂ fuel. Reactivity determination was by period measurement with various control rod configurations. The temperature range covered was 22-75°C.

The Cornell University Zero Power Reactor was studied over a temperature range 5-70°C for water-to-fuel ratios of 1:1, 2:1, and 3:1. After clearly establishing that the 4:1

^{3/} J. R. Brown, et al., "Reactor Properties of Water Moderated Slightly Enriched Uranium Lattices," WAPD-117, p. 117
Westinghouse Atomic Power Division (1954).

 $[\]frac{4}{}$ J. R. Brown, <u>et al.</u>, "Kinetic and Buckling Measurements on Lattices of Slightly Enriched Uranium or UO₂ Rods in Light Water," WAPD-176, p. 39 Westinghouse Atomic Power Division (1958).

^{5/} P. W. Davison, et al., "Yankee Critical Experiments-Measurements on Lattices of Stainless Steel Clad Slightly Enriched Uranium Dioxide Fuel Rods in Light Water." YAEC-94, p. 7'
Yankee Atomic Electric Company (1959).

Sec. 1.2 - 1.3

lattice had a positive isothermal coefficient of reactivity with no indication of going negative, the study of this core was terminated at a maximum temperature of 45°C. The accuracy of the values of α for both the Westinghouse and Cornell experiments is about $\frac{1}{2}$ 0.03 ¢/°C, and this accuracy is nearly independent of the value of α .

1.3 TEMPERATURE DEPENDENT DISADVANTAGE FACTORS

The neutron density disadvantage factor δ_n and the experimentally measured disadvantage factor δ_{exp} are defined by the ratios $\delta_n = \overline{N}^m/\overline{N}^f$ and $\delta_{exp} = \overline{C}^m/\overline{C}^f$ where \overline{N} and \overline{C} are respectively the spatially averaged neutron density and foil count rate per unit volume; superscripts m and f indicate respectively the moderator and fuel regions of the reactor.

Disadvantage factor measurements have previously been made on cores similar to the Cornell critical assembly. The Brookhaven measurements $\frac{6,7,8,9,10}{}$ were made with dysprosium

^{6/} H. Kouts, "Intra-cell Flux Traverses," BNL-1783,
Brookhaven National Laboratory (1953).

H. Kouts, "Intracell Flux Traverses and Thermal Utilization for 1.15% Enriched Uranium Rods in Ordinary Water," BNL-1982, Brookhaven National Laboratory (1954).

^{8/} G. A. Price, "Thermal Utilization Measurement," BNL-1992, Brookhaven National Laboratory (1954).

pellets distributed through the fuel and moderator regions. The pellets were 1/16-inch diameter, 0.007-inch thick foils made from a mixture of $\mathrm{Dy}_2\mathrm{O}_3$ with aluminum or plastic. Numerical integration of the detailed flux maps gave average count rates for each region which were converted to experimental disadvantage factors. An uncertainty of about 2% was assigned from data scatter; statistical uncertainty in counting was about 1%.

The Westinghouse disadvantage factor measurements $\frac{11,12}{}$ were made with uranium sector foils cut and placed in the fuel and moderator regions of the reactor. The foil was highly enriched U^{235} dispersed in aluminum to match the fuel U^{235} atom density. These foils were gamma-counted for fission product activity. The experimental disadvantage factor was obtained directly as the ratio of count rates per unit volume of the moderator and fuel sector foils. The uncertainty in the measurement was about 3%.

^{9/} H. J. Kouts, et al., "Intracell Flux Traverses and Thermal Utilization, 1.027% Enriched Uranium Rods in Light Water," BNL-1796, Brookhaven National Laboratory (1954).

^{10/} H. C. Honeck, "The Calculation of Thermal Utilization and Disadvantage Factors in Uranium/Water Lattices," Nuc. Sci. Eng. 18, 49 (1964).

No previously published works indicate that the temperature dependence of the disadvantage factor has been studied experimentally. MacVean's recently developed method of calculating thermal lattice parameters $\frac{13}{}$ gives the temperature dependence of the disadvantage factor. Since the calculated changes are of the order of 10^{-3} /°C an experimental method was required which was more accurate than those previously used.

Experimental disadvantage factors were measured for three water-to-fuel ratios over a temperature range 5-65°C. An integral foil counting method was used employing a 0.600 $\frac{1}{2}$ 0.001-inch diameter foil in the fuel and an appropriately shaped moderator foil. Five-mil thick foils of dysprosium (5.24% dysprosium in aluminum), manganese (P-metal), and vanadium were chosen because their cross sections are nearly 1/v. Two counting methods were used. One was to dissolve the manganese foils in nitric acid and gamma-count aliquots of the solutions in a well-type scintillation counter. The other method was to beta-count the solid foils in a proportional flow counter. Results of the two methods agreed within the statistical errors which were about 0.7%.

^{11/} A. Z. Kranz, "Measurements of Thermal Utilization Resonance Escape Probability, and Fast Fission Factor of Water Moderated Slightly Enriched Uranium Lattices," WAPD-134, Westinghouse Atomic Power Division (1955).

 $[\]frac{12}{}$ A. Z. Kranz and G. G. Smith, "A Second Report on Measurements of f, p, and ϵ of Water Moderated Slightly Enriched Uranium Lattices," WAPD-151, Westinghouse Atomic Power Division (1956).

 $[\]frac{13}{}$ C. R. MacVean, footnote 2, pp. 143-145.

CHAPTER 2

THEORETICAL CALCULATION OF THE ISOTHERMAL TEMPERATURE COEFFICIENT OF REACTIVITY

2.1 INTRODUCTION

A calculation of the isothermal temperature coefficient of reactivity was made using two group, two region perturbation theory. The presentation here follows closely that of Larrimore. $\frac{14}{}$

Section 2.2 presents and discusses the two group, two region neutron balance equations and the associated boundary conditions necessary for the solution. The bilinearly weighted, first order reactivity equations from perturbation theory are given for the core, reflector, and interface regions of the reactor. In these latter equations, temperature derivatives of the reactor parameters are weighted by the fluxes, adjoint fluxes, flux gradients, and adjoint flux gradients. The temperature derivatives are discussed in Sec. 2.3. Utilization of these equations for machine calculations is discussed in Sec. 2.4.

^{14/} J. A. Larrimore, "Temperature Coefficients of Reactivity in Homogenized Thermal Nuclear Reactors," Ph.D. Thesis, pp. 185-211, M.I.T. (September, 1962).

2.2 TWO GROUP, TWO REGION EQUATIONS

2.2.1 Steady State Neutron Balance Equations

The steady state neutron balance equations for the core region of the reactor are:

$$(D_{1c}^{\nabla^2 - \Sigma_{1c}}) \varphi_{1c} + ve\Sigma_{fis} \varphi_{2c} = 0$$
 (2.1)

$$p\Sigma_{1c}\phi_{1c} + (D_{2c}\nabla^2 - \Sigma_{2c}) \phi_{2c} = 0$$
 (2.2)

Analogous equations for the reflector are:

$$(D_{1r}\nabla^2 - \Sigma_{1r}) \varphi_{1r} = 0 \qquad (2.3)$$

$$\Sigma_{1r} \varphi_{1r} + (D_{2r} \nabla^2 - \Sigma_{2r}) \varphi_{2r} = 0$$
 (2.4)

where: subscript 1 refers to the fast group, subscript 2 refers to the thermal group, subscript c denotes the core, subscript r denotes the reflector, D is the diffusion constant for a given group and region, Σ_1 is the fast group removal cross section, $\Sigma_{\rm fis}$ is the fission cross section, Σ_2 is the thermal absorption cross section, ∇ is the average number of neutrons per thermal fission, ε is the fast fission factor. ∇^2 is the Laplacian differential operator, and p is the resonance escape probability.

The adjoint equations for the core and reflector are given by

$$(D_{1c}\nabla^{2} - \Sigma_{1c}) \varphi_{1c}^{\dagger} + p\Sigma_{1c}\varphi_{2c}^{\dagger} = 0$$
 (2.5)

$$ve\Sigma_{fis}\phi_{1c}^{\dagger} + (D_{2c}\nabla^{2} - \Sigma_{2c}) \phi_{2c}^{\dagger} = 0$$
 (2.6)

$$(D_{1r}\nabla^{2}-\Sigma_{1r}) \varphi_{1r}^{+} + \Sigma_{1r}\varphi_{2r}^{+} = 0$$
 (2.7)

$$(D_{2r}\nabla^2 - \Sigma_{2r}) \varphi_{2r}^+ = 0$$
 (2.8)

where the superscript + indicates the adjoint flux functions

Boundary conditions at the outer extrapolated boundary require that the fast and slow fluxes and adjoint fluxes vanish. At the core-reflector interface the boundary conditions require that fast and slow fluxes and adjoint fluxes match (i.e. $\phi_{1c} = \phi_{1r}, \phi_{1c}^+ = \phi_{1r}^+$, and similar equations with the 1 replaced by 2), and that the fast and slow currents and adjoint currents match (i.e. D_{ic} $\phi_{ic} = D_{ir}$ ϕ_{ir} where i is either 1 or 2, and the same expressions are written for the the adjoint fluxes).

2.2.2 Bilinearly Weighted Reactivity Relations

Once the fast and slow fluxes and adjoint fluxes for the core and reflector are known, they can be used in the standard two group, two region, first-order perturbation theory reactivity equations. Perturbations of the parameters are equated to temperature derivatives of the parameters, and the reactivity effects are calculated.

The following expression is given by Larrimore $\frac{15}{}$ for the core contribution to the isothermal temperature coefficient, α_c :

 $[\]frac{15}{}$ J. A. Larrimore, footnote 14, p. 191.

$$\alpha_{\mathbf{c}} = \left(\int_{\mathbf{c}} d\mathbf{r} \, \phi_{1\mathbf{c}}^{\dagger} \, v \in \mathbb{Z}_{fis} \phi_{2\mathbf{c}} \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-\nabla \phi_{1\mathbf{c}}^{\dagger} \, \cdot \right] \right)^{-1} \cdot \left(\int_{\mathbf{c}} d\mathbf{r} \, \left[-$$

where $d\underline{r}$ is the volume element, the subscript c on the integral sign implies integration over the core of the reactor, and θ is temperature.

Similarly, the reflector contribution, $\alpha_{\mbox{\scriptsize r}}$, is given by Larrimore $^{\mbox{\scriptsize 16}/}$ as

$$\alpha_{\mathbf{r}} = \left(\int_{\mathbf{c}}^{\mathbf{d}\mathbf{r}} \phi_{1\mathbf{c}}^{\dagger} v \in \Sigma_{\mathbf{fis}} \phi_{2\mathbf{c}} \right)^{-1} \cdot \left(\int_{\mathbf{r}}^{\mathbf{d}\mathbf{r}} \left[-\nabla \phi_{1\mathbf{r}}^{\dagger} \cdot \frac{d\Sigma_{1\mathbf{r}}}{d\theta} \nabla \phi_{1\mathbf{r}} - \nabla \phi_{2\mathbf{r}}^{\dagger} \cdot \frac{dD_{2\mathbf{r}}}{d\theta} \nabla \phi_{2\mathbf{r}} - \phi_{1\mathbf{r}}^{\dagger} \frac{d\Sigma_{1\mathbf{r}}}{d\theta} \phi_{1\mathbf{r}} \right) + \phi_{2\mathbf{r}}^{\dagger} \frac{d\Sigma_{1\mathbf{r}}}{d\theta} \phi_{1\mathbf{r}} - \phi_{2\mathbf{r}}^{\dagger} \frac{d\Sigma_{2\mathbf{r}}}{d\theta} \phi_{2\mathbf{r}} \right) \cdot (2.10)$$

^{16/} J. A. Larrimore, footnote 14, p. 194.



Finally, Larrimore gives for α_i , the interface effect, $\frac{17}{}$

$$\alpha_{i} = \left(\int_{c}^{d} d\underline{r} \, \phi_{1c}^{+} \, v \in \Sigma_{fis} \, \phi_{2c}\right)^{-1} \cdot \left[-\nabla \phi_{1r}^{+} \cdot \nabla \phi_{1c} (D_{1c} - D_{1r})\right]$$

$$-\nabla \phi_{2r}^{+} \cdot \nabla \phi_{2c} (D_{2c} - D_{2r}) - \phi_{1r}^{+} \phi_{1c} (\Sigma_{1c} - \Sigma_{1r})$$

$$+ \phi_{2r}^{+} \phi_{1c} (p \Sigma_{1c} - \Sigma_{1r})$$

$$+ \phi_{1r}^{+} \phi_{2c} \, v \in \Sigma_{fis} - \phi_{2r}^{+} \phi_{2c} (\Sigma_{2c} - \Sigma_{2r})\right]_{int}$$

$$[dV/d\theta] \qquad (2.11)$$

where all the functions in the second set of brackets are evaluated at the core-reflector interface, and $dV/d\theta$ is the change of core volume with temperature. For an infinite cylinder, $dV/d\theta$ is given by

$$dV/d\theta = 2\pi r^2 \beta_{a1}/3$$
 (2.12)

where r is the core radius, and β_{al} is the volumetric coefficient of thermal expansion of aluminum.

 $[\]frac{17}{J}$ J. A. Larrimore, footnote 14, p. 209.

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The total isothermal temperature coefficient for the reactor is the sum of the core, reflector, and interface contributions:

$$\alpha = \alpha_{c} + \alpha_{r} + \alpha_{i} \qquad (2.13)$$

2.3 TEMPERATURE DERIVATIVES OF THE NUCLEAR PARAMETERS

In order to calculate the various expressions for the isothermal temperature coefficient, it is necessary to have relations for the temperature derivatives of the various nuclear parameters, viz., v, ε , p, and the various D's and Σ 's.

2.3.1 Reflector Group Constants

The temperature derivative of the macroscopic cross section Σ is easily found by differentiating

$$\Sigma = N_{a} \sigma , \qquad (2.14)$$

where N_a is the number density of atoms whose microscopic cross section is σ to give

$$(1/\Sigma)d\Sigma/d\theta = (1/N_a)dN_a/d\theta + (1/\sigma)d\sigma/d\theta . \qquad (2.15)$$

Since $N_{\rm a}$ is proportional to the density d of the material, it follows that

$$(1/N_a) dN_a/d\Theta = -\beta , \qquad (2.16)$$

where β is the volumetric coefficient of thermal expansion for the material. By substitution in Eq. (2.15), the temperature derivative of Σ becomes

$$(1/\Sigma) d\Sigma/d\Theta = -\beta + (1/\sigma) d\sigma/d\Theta . \qquad (2.17)$$

For the fast group, it was assumed that the microscopic cross section does not change with temperature. This assumption leaves only a density effect term for the fast-group macroscopic cross section temperature derivative. For the reflector we therefore have

$$(1/\Sigma_{1r})d\Sigma_{1r}/d\theta = -\beta_{H_20}$$
 (2.18)

The slow microscopic cross section for water σ_{2r} is proportional to 1/v; hence it is proportional to $\theta^{-1/2}$. Therefore,

$$(1/\sigma_{2r})d\sigma_{2r}/d\theta = -0.5/\theta$$
 (2.19)

where θ is in °K. For the slow group in the reflector, Eq. (2.17) therefore becomes:

$$(1/\Sigma_{2r})d\Sigma_{2r}/d\Theta = -\beta_{H_2O}-0.5/\Theta$$
 (2.20)

The diffusion constant D can be written

$$D = 1/(3\Sigma_{rr}) , \qquad (2.21)$$

where $\boldsymbol{\Sigma}_{\text{tr}}$ is the appropriate transport cross section.

Logarithmic differentiation gives

$$(1/D)dD/d\theta = +\beta - d\sigma_{tr}/d\theta . \qquad (2.22)$$

Larrimore $\frac{18}{}$ gives the following relationship for the logarithmic slope of the thermal transport cross section of water:

$$(1/\sigma_{tr})d\sigma_{tr}/d\Theta = -n/\Theta , \qquad (2.23)$$

where n is given for 20, 50, and 100°C as 0.473, 0.471, and 0.469 respectively. Using the value for 50°C, Eq. (2.22) becomes

$$(1/D_{2r})dD_{2r}/d\Theta = \beta_{H_2O} + 0.471/\Theta$$
 (2.24)

Assuming again that the microscopic cross section of the fast group does not change with temperature, Eq. (2.22) for the fast group becomes

$$(1/D_{1r})dD_{1r}/d\theta = \beta_{H_20}$$
 (2.25)

2.3.2 Core Group Constants

In the core region of the reactor, the fast group macroscopic cross section $\boldsymbol{\Sigma}_{\mathbf{C}}$ can be written

$$\Sigma_{c} = (V^{f} + V^{m})^{-1} (V^{f} \Sigma_{f} + V^{m} \Sigma_{m})$$
 (2.26)

 $[\]frac{18}{\text{J. A. Larrimore, footnote 14, pp. 83-84}}$

where V^f and V^m are the volumes of the fuel and moderator region of the cell, Σ_f is the fuel cross section, and Σ_m is the moderator cross section.

For the fast group, the microscopic cross sections are assumed not to vary with temperature, and the expansion of the fuel is taken to be negligible compared to the expansion of the cladding. The logarithmic temperature derivative of Σ_{1c} then becomes

$$(1/\Sigma_{1c})d\Sigma_{1c}/d\Theta = V^{m}(V^{f}+V^{m})^{-1}(\Sigma_{1r}/\Sigma_{1c})\left[(2\beta_{A1}/3)-\beta_{H_{2}O}\right],$$

$$(2.27)$$

where β_{A1} is the volumetric coefficient of thermal expansion of aluminum, the cladding material. The last term in Eq. (2.27) arises because the density effect on the moderator is the combined expansion effects of the water and aluminum For the reactor cell, it is only the water cross-sectional area change per unit length of the reactor cell which contributes to the water density change. This area change is due to the expansion of aluminum structural members. The $2\beta_{A1}/3$ term accounts for this area change per unit length.

Using Eq. (2.21) where, for the fast group,

$$\Sigma_{tr} = (V^{f} + V^{m})^{-1} (V^{m} \Sigma_{tr}^{m} + V^{f} \Sigma_{tr}^{f}) ,$$
 (2.28)

it can be shown that the logarithmic temperature derivative of $\mathrm{D}_{1\,\mathrm{C}}$ is

$$(1/D_{1c})dD_{1c}/d\theta = (D_{1c}/D_{1r})(V^{m})(V^{f}+V^{m})^{-1}(\beta_{H_{2}O}-2\beta_{A1}/3)$$
 (2.29)

The temperature derivatives for the slow group core parameters were taken from calculations by MacVean using the computer program COUTH, "a simplified polyenergetic cell theory (which) is formulated to determine spatially averaged energy dependent thermal fluxes in the moderator, cladding, and fuel regions within the unit cell of a reactor lattice. The derived spectra are then utilized in the calculations of the thermal integral parameters and average cross sections required for reactor computations "19/" Calculations at two temperatures provide the temperature dependence of the thermal parameters used here

2.3.3 Resonance Escape Probability

The resonance escape probability temperature derivative can be calculated by the following scheme. Weinberg and Wigner $\frac{20}{}$ give the following expression for p(E), the resonance escape probability to energy E from source energy E_s :

 $[\]frac{19}{C}$. R. MacVean, footnote 2, p. ii

^{20/} A. M. Weinberg and E. P. Wigner, The Physical Theory of

Neutron Chain Reactors, p. 301. University of Chicago

Press, Chicago (1959)

$$p(E) = \exp \left[-(1/\xi) \int_{E}^{E_s} a(E') \sum_{s} (E') + \sum_{s}]^{-1} dE' / E' \right],$$
(2.30)

where ξ is the average lethargy increase per collision, Σ_a is the energy dependent absorption cross section of the cell, and Σ_s is the scattering cross section of the cell. Equation (2.31) is rewritten in the usual form

$$p = \exp -N_u(\xi \Sigma_s)^{-1} Rl_{eff}$$
 (2.31)

where $\mathrm{RI}_{\mathrm{eff}}$ is the effective resonance integral, and N_{u} is the homogenized fuel atom density in the cell.

Logarithmic differentiation with respect to temperature results in the following expression

$$(1/p)dp/d\theta = -N_uRI_{eff}(\epsilon_s)^{-1}[1/N_u)dN_u/d\theta - (1/\Sigma_s)d_s/d\theta +$$

$$(1/RI_{eff})dRI_{eff}/d\Theta$$
 (2.32)

The atomic density of the fuel varies with temperature however, since fuel atoms are lost from the cell only through axial expansion of the fuel, we have

$$(1/N_u) dN_u/d\Theta = -B_u/3$$
 (2.33)

The microscopic scattering cross section is a constant, therefore the scattering cross section temperature derivative is given by

$$(1/\Sigma_{S}) d\Sigma_{S}/d\theta = -\beta_{S} . \qquad (2.34)$$

The scatterer is water and is lost from the cell by expansion of water, but is gained in the cell as the horizontal cross-sectional area of the cell increases due to aluminum structural expansion. The density change in the moderator is therefore a combination of water and aluminum expansion, and

$$(1/\Sigma_s) d\Sigma_s / d\Theta = -\beta_{H_2O} + (2/3)\beta_{A1}$$
 (2.35)

Using Eqs. (2.33) and (2.35), Eq. (2.32) can be rewritten as follows

$$(1/p)dp/d\theta = -N_uRI_{eff}(\xi\Sigma_s)^{-1} \left[\beta_{H_2O} - \frac{2}{3}\beta_{A1} - \frac{1}{3}\beta_u + (1/RI_{eff})dRI_{eff}/d\theta\right]$$
 (2.36)

Table 2.1 gives the values of the terms in Eq. (2.36) for the water-to-fuel ratios investigated.

2.3.4 Fast Fission Factor

An estimate of the temperature effect on the fast fission factor can be made using an empirical relation for the fast fission factor for ${\rm UO}_2$ -water lattices as given by Larrimore: $\frac{21}{}$

 $[\]frac{21}{J}$ J. A. Larrimore, footnote 14, p. 145.



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$$(1/\Sigma_{S}) d\Sigma_{S}/d\theta = -\beta_{S} . \qquad (2.34)$$

The scatterer is water and is lost from the cell by expansion of water, but is gained in the cell as the horizontal cross-sectional area of the cell increases due to aluminum structural expansion. The density change in the moderator is therefore a combination of water and aluminum expansion, and

$$(1/\Sigma_s) d\Sigma_s / d\Theta = -\beta_{H_2O} + (2/3)\beta_{A1}$$
 (2.35)

Using Eqs. (2.33) and (2.35), Eq. (2.32) can be rewritten as follows

$$(1/p)dp/d\theta = -N_u RI_{eff} (\xi \Sigma_s)^{-1} [\beta_{H_2O} - \frac{2}{3} \beta_{A1} - \frac{1}{3} \beta_u + (1/RI_{eff})dRI_{eff}/d\theta]$$
 (2.36)

Table 2.1 gives the values of the terms in Eq. (2.36) for the water-to-fuel ratios investigated.

2.3.4 Fast Fission Factor

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 $[\]frac{21}{J}$ J. A. Larrimore, footnote 14, p. 145.



TABLE 2.1

VALUES OF PARAMETERS USED IN THE CALCULATION OF 1/p)dp/d0

Water to fuel ratio	$\frac{N_0RI_{eff}}{\xi\Sigma_s}$	$\sqrt{q}^{n}\theta$	$\beta_{A1} = \frac{c}{a}$	dRI _{eff} /d0 Rleff	$^{\beta}_{\text{H}_2}$ 0	$^{\text{d}}_{\text{H}_2\text{O}} = \frac{\text{d}}{\text{p}} / \frac{\text{d}}{\text{p}}$
		(10-4/°C)	$(10^{-4}/^{\circ}C)$ $(10^{-4}/^{\circ}C)$ $(10^{-4}/^{\circ}C)$	(10 ⁻⁴ /°C)	(10 ⁻⁴ /°C)	(10 ⁻⁴ /°C) (10 ⁻⁴ /°C) (©20°C)
1::1	0.249	0.3	0.75	1,42	2.05	-0.74
2:1	0.132	0.3	0.75	1.42	2.05	-0.39
3:1	060.0	0.3	0.75	1,42	2.05	-0.27
4:1	690°0	0.3	0.75	1,42	2.05	-0.20

B. Cady, personal communication (June, 1964). la/

Harold Etherington (Editor), Nuclear Engineering Handbook, p. 10-18, McGraw-Hill Book Company, Inc., New York (1958). /q

C. D. Hodgman (Editor-in-Chief), Handbook of Chemistry and Physics, 42nd ed., p. 2239. Chemical Rubber Publishing Co., Cleveland, Ohio (1960).0

d/ ibid., p. 2143.



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$$\epsilon - 1 = (0.1565)[1 + 0.875(d_{H_2O} V^m/V^f) + 0.288 V^s/V^f]^{-1}$$
 (2.37)

where ϵ is the fast fission factor, d_{H_2O} is the water density, and V^S is the volume of the structural materials. Logarithmic differentiation, assuming V^S/V^f to be small, gives

$$(1/\epsilon)d\epsilon/d\theta = 5.59(V^{m}/V^{f})(\epsilon-1)^{2}(\epsilon)^{-1}[(2\beta_{H_{2}O}/3)-\beta_{u}/3].$$
 (2.38)

Using these values for the 1:1 core: $\epsilon = 1.03$, $V^m/V^f = 1.012$, $\theta = 20^{\circ}\text{C}$, $\beta_{\text{H}_20} = 2.05\text{x}10^{-4}/^{\circ}\text{C}$, and $\beta_u = 0.3\text{x}10^{-4}/^{\circ}\text{C}$, the temperature effect on ϵ as calculated by Eq. (2.38) is found to be $0.6\text{x}10^{-6}/^{\circ}\text{C}$. For all other cores ϵ is smaller than 1.03 and the $(\epsilon-1)^2$ term is dominant. The fast fission factor temperature dependence is therefore found to be negligible.

2.3.5 <u>Discussion of the Temperature Derivatives of the Nuclear</u> Parameters

Temperature derivatives of the nuclear parameters have two major contributions: one which is directly related to temperature change (such as the variation of the microscopic cross sections for the slow group) and one which is indirectly related to the temperature change by the effect which this temperature change has on the thermal expansion of the materials in the reactor. Over the investigated temperature range, the temperature derivatives of the microscopic cross sections change by about 10%. Over the same temperature interval, the value of

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 β_{A1} and β_{u} are constant, and $dRI_{eff}/d\theta$ changes by about 3%. Therefore, there are some terms in the expression for the temperature coefficient of reactivity which do not change appreciably over the temperature interval studies. Over this same temperature range, the value of β_{H_20} changes from about $0.5 \times 10^{-4}/^{\circ} C$ to about $6.0 \times 10^{-4}/^{\circ} C$.

The above discussion suggests an expression for α of the form

$$\alpha = A + B \beta_{H_2O} \qquad (2.37)$$

Calculated values of A and B are tabulated in Table 2.3 in the next subsection. The experiments described in Chapter 3 showed the predicted linear dependence although the calculated and observed values of A and B did not agree for all water-to-fuel ratios.

2.4 NUMERICAL CALCULATION OF THE ISOTHERMAL TEMPERATURE COEFFICIENT OF REACTIVITY

A computer program was developed by $0sias^{22}$ which solves the neutron balance equations, calculates the fluxes and adjoint fluxes, and calculates the isothermal temperature coefficient of reactivity by Eqs. (2.9)-(2.11) for an

 $[\]frac{22}{}$ D. J. Osias, private communication (August, 1964).

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infinite cylinder reactor Calculations were made at 4, 20, 40, 60, and 80°C. These calculations represent an approximation to the first order perturbation theory in that the flux shapes calculated at 20°C were used to compute the temperature coefficient at all other temperatures. All parameters of the two group two region problem change with temperature on the order of 10⁻⁴/°C, so that changes in the flux shapes with temperature are expected to contribute an error of less than 1% to the calculated values of the isothermal temperature coefficient of reactivity.

The input numbers required and their sources are listed in Table 2.2. Results of the computer calculation are given in Table 2.3 for the five water-to-fuel ratios of the reactor. The calculated values of α are a linear function of $\beta_{\rm H_2O}$.

TABLE 2.2

				Water-to-Fuel	Fuel Rati	0	
Parameter	Unit	1:1	1,5:1	2:1	-	4:1	Reference
o t	cm ²	42.0	32.0	29.8	29.3	29.0	B
$^{\Sigma}1^{ m c}$	cm ⁻¹	0.028	0.0385	0.0393	0.0410	0.0413	ਲ
>		2,43	2,43	2.43	2.43	2.43	Ą
(i)		1.03	1.023	1.019	1,015	1.013	р
$^{\Sigma}$ fis	cm	0.05996	0.0524	0.0455	0.0352	0.0282	U
d		0.765	0.83	0.867	0.907	0.928	Ъ
D_{2c}	cm	0.370	0,311	0.277	0.24	0.2206	U
$^{\square}2^{c}$	cm 1	0.09173	0,083	0.0747	0.0622	0,0535	O
D_{1r}	cm	1.22	1.22	1.22	1.22	1.22	d
$^{\mathbb{Z}}_{1\mathbf{r}}$	cm ⁻¹	670.0	6,00.0	0.049	0.049	0.049	Ф
$^{\mathrm{D}_{2r}}$	сш	0.140	0.140	0.140	0.140	0.140	O
$^{\mathbb{Z}}2^{\mathbf{r}}$	cm ⁻¹	0.01881	0.01881	0.01881	0.01881	0.01881	U
$(1/\Sigma_{ extsf{fis}})(d\Sigma_{ extsf{fis}}/d\Theta)$	10-4/°C	-7.76	-8.87	44.6=	99.6-	7.6	O
$(1/\Sigma_{2c})(d\Sigma_{2c}/d\theta)$	J°/*-01	-7.69	-8.97	. 6 . 83	-10,6		O
$(1/D_{2c})(dD_{2c}/d\theta)$	10-4/°C	3.2	67° 7	5.76	7,27	8 . 38	O
, ,	СШ	24,40	21,39	21,01	22,47	26,02	þ

a/ L. J. Templin, "Reactor Physics Constants," 2nd ed., ANL 5800, pp. 145-150.

Argonne National Laboratory (1963).

b/ S. S. Berg, footnote 1, p. 151.

c/ C. R. MacVean, footnote 2, pp. 143-149



TABLE 2.3

		C	CALCULATED VALUES		OF α_c , α_r ,	α_{i} , A_{i}	AND B		
W/F	Φ	$^{\beta}_{\text{H20}} = ^{a/}$	/d p	arb/	α_{i}^{b}	/ <mark>q</mark> \(\ni_{\infty}\)	Beff C/	A	В
	၁	10-4/°C	J°/Þ	J°/Þ	J°/4	J 0/ Þ	%	J°/\$	104¢
 	20 40 60 80	0 2.05 3.90 5.32 6.65	-0.438 -1.418 -2.301 -2.980	0.174 0.157 0.141 0.127 0.114	0.032 0.032 0.032 0.032 0.32	0.232 1.229 2.128 -2.821 -3.470	0.7943	-0,232	0.487
5 , 1	4 20 40 60 80	0000	-0,236 -0,920 -1,536 -2,010	0 146 0 131 0 116 0 104 0 092	0.058 0.058 0.058 0.058	0.032 0.731 1.362 1.849	0,8692	-0,032	±0,342
2 ° 1	20 40 60 80	0 2.05 3.90 5.32 6.65	0.083 -0.545 -1.111 -1.547	0.111 0.100 0.088 0.078 0.070	090.0	0.254 -0.385 -0.963 -1.409	0.8630	0.254	0.313
3.1	77 70 70 80 80	0 2.05 3.90 5.32 6.65	0.750 0.198 -0.300 -0.683	0.090 0.080 0.071 0.062 0.062	0.074 0.074 0.074 0.074 0.074	0.914 0.352 -0.155 -0.547	0.8330	0.914	.0.274

continued on next page

Table 2.3 continued

-0.240
1.538
0.7955
1.538 1.047 0.603 0.264
0.073 0.073 0.073 0.073 0.073
0.064 0.056 0.050 0.045
1,402 0,918 0,480 0,146 -0,168
0 2.05 3.90 5.32 6.65
40 40 60 80
4:1

C. D. Hodgman (Editor-in-Chief), Handbook of Chemistry and Physics, 42nd ed., p. 2143, Chemical Rubber Publishing Co., Cleveland, Ohio (1960).

 $D_{\,^{\circ}}$ J. Osias, private communication (September, 1964). <u>P</u>

 $\frac{c}{}$ S. S. Berg, footnote 1, p. 210.



CHAPTER 3

METHODS AND RESULTS OF THE ISOTHERMAL TEMPERATURE COEFFICIENT EXPERIMENT

3.1 GENERAL EXPERIMENTAL PROCEDURE

A typical series of runs for the temperature coefficient experiment was made by starting at the coldest temperature and progressing to higher temperatures in steps of five or ten degrees. Smaller temperature intervals were used in the region where the isothermal coefficient changed sign.

Temperature measurements were made at three times during a run: at startup, at approximately half power, and at maximum power. The average of these temperatures was assigned to the run.

All control rods were at the fully withdrawn position and the source was removed from the core prior to collecting data on the stable period of the clean core. Data were collected over approximately three decades increase in power level.

After the final temperature measurement, the water was removed from the reactor tank to the dump storage tank, heated, and returned to the reactor tank for the run at the next higher temperature.

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3.2 TEMPERATURE REGULATION AND MEASUREMENT

3.2.1 Water Heating

When the reactor is shut down, the moderator water is stored in the dump storage tank located just below the reactor tank. The reactor tank capacity is 2,000 gallons; that of the dump tank is 2,200 gallons. A steam heater in the dump storage tank was used to heat the water at the rate of about one-half degree centigrade per minute. Since the system lacks automatic temperature control, it was difficult to obtain or maintain a given temperature to within one or two degrees.

3.2.2 Water Chilling

The recirculation pump for the reactor demineralizer system circulated the water from the dump storage tank through a Worthington water chiller $\frac{23}{}$ (model RWW-400) and back to the dump storage tank. The cooling rate was approximately one-half degree centigrade per hour. Because of this slow cooling rate, a series of experimental runs was made in steps of increasing temperature. The lowest obtainable temperature was found to be about 5°C .

3.2.3 Temperature Measurement

Four twenty-gauge Leeds and Northrup (#58-1) asbestos insulated, fiberglass sheathed chromel-alumel thermocouples placed in the core through interstitial holes in the top grid

 $[\]frac{23}{}$ On loan from the Department of Thermal Engineering.



plate were used to measure the moderator temperature. Sampling of the temperature took place at radii and depth as given in Table 3.1.

TABLE 3.1
THERMOCOUPLE POSITIONS

Water-to- Fuel Ratio	Thermocouple 1	Thermocouple 2	Thermocouple 3	Thermocoup. 5
1:1 radius ^{a/}	1.75-IV	2.5-IV	8.5-II	7.0-IV
depth	36	18	36	24
2:1 radius	4.75-11	5 .0 ~ III	9.5×111	2.25~IV
depth	30	24	12	36
3:1 radius	7 5-IV	2.5-IV	7 , 5 - I	5.0-III
depth	29	25	18	36
4:1 radius	8 . 75 - II	C /	2.5-IV	9.75-III
depth	18		18	18

a/ Measured in inches from the center of the core. Roman numerals indicate the grid plate sector.

The ice junction was located in the reactor cell next to the reactor, and copper multiconductor cable was used to bring the thermocouple voltages into the control room. A precision potentioneter (Leeds and Northrup model 8662) was used to measure the voltages to $\frac{1}{2}$ 0.001 mV which corresponds to $\frac{1}{2}$ 0.025°C.

Measured in inches down from the top of the upper grid plate
The horizontal midplane of the fueled region of the core is
at 30.5 inches.

This thermocouple was located in the reactor fill pipe for this water-to-fuel ratio.

Sec. 3 2 30

3.2.4 Temperature Uniformity

The time required for a step temperature difference between the cladding and the center of the fuel rod to decay to less than 20% was computed to be of the order of three minutes. This analysis was made using the standard Fourier charts for transient heat transfer in cylinders. Helium fills the void between the fuel pellet (o.d. 0.600±0.003 inches) and the cladding (i.d. 0.610±0.002 inches). The effect of this void was included in the calculations by assuming that the fuel pellet does not touch the cladding. This assumption results in an overestimate of the transient decay time inasmuch as conductive heat transfer from the pellet to the cladding has been neglected. The fuel pellet properties used in this calculation were:

fuel density 10.6 gm/cm³
thermal conductivity 0.07 watts/cm²C
thermal capacity 0.063 cal/gm²C

The time required to take the reactor critical is several times the three minute interval mentioned above. About fifteen minutes are needed to pump the water into the reactor tank from the dump storage tank. The reactor tank fill pump was usually run for several minutes after the reactor tank was full in order to agitate the water in the reactor tank. Another eight minutes are required to raise the control rods. Therefore, normal startup procedure allowed sufficient time to establish



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thermal equilibrium in the reactor tank; the maximum observed temperature difference between thermocouples was less than $\frac{1}{4}$ °C.

3.3 PERIOD MEASUREMENT

Following the establishment of a good temperature profile, the reactor was taken on a positive period by removal of all control rods. With the control rods withdrawn, the reactor is in a clean configuration because the fuel followers in the control rod elements are then at the same height as the fueled section of the normal fuel rods.

Reactivity errors resulting from positioning errors should be small because the differential control rod worth is a minimum at the fully withdrawn position. The reactivity effect of a simultaneous one-inch misalignment of all four control rods was found to be about 0.2¢, which is within the statistical uncertainty of the measurement. The specifications for the digital indicating system for control rod position call for position reproducibility to within 0.05 inch. Therefore, misalignment of the control rods at the fully withdrawn position will contribute a negligible reactivity error, certainly less than 0.1¢.

Time dependent flux transients associated with control rod motion or source removal decay rapidly so that the actual reactor period is within one per cent of the stable reactor period after two periods have elapsed. To allow transients

^{24/} L. J. Templin, "Reactor Physics Constants," ANL-5800, 2nd ed., p. 463. Argonne National Laboratory (1963).



Sec. 3.3

to decay, the data recording system was not started until the power level had increased beyond that at criticality by about one decade, which is more than two periods in time.

The suitable range of periods was from 25 to 100 seconds. Periods less than 25 seconds are too short to measure satisfactorily. Lack of temperature control of the water in the reactor tank prevented the use of periods much longer than 100 seconds at temperatures much different from room temperature because temperature drifts cause corresponding reactivity drifts. To avoid problems associated with very long or very short periods, the excess reactivity of the clean core was kept between about 7¢ and about 25¢ by adding or removing peripheral fuel rods. This technique was chosen rather than that of compensating with control rods because with the control rods fully withdrawn, systematic errors due to control rod positioning and to temperature effects on control rod worth were avoided.

Two BF $_3$ pulse counters (Hammer-20th Century 31EB70G) provided the data for the period determination. The outputs of these counters were recorded automatically by a Hamner Spectrometer, a combination scaler-timer-printer. $\frac{25}{}$ The data recording cycle was adjusted so that several data points were recorded during the time interval of one period. The

^{25/} S. S. Berg, footnote 1, p. 104.



Sec. 3.3 - 3.4

detectors themselves were positioned in the reactor instrument thimbles so that saturation did not occur for power levels used.

3.4 DATA REDUCTION

Period measurement raw data were analyzed by the computer code RHOFIT, $\frac{26}{}$ a least squares fit to an exponential function. The computed period is then fed into a subroutine which calculates the excess reactivity by the inhour equation

$$\rho_{\text{ex}}/\beta_{\text{eff}} = \sqrt{(\beta_{\text{eff}}T)^{-1}} \sum_{i=1}^{6} (\beta_{i}/\beta_{\text{eff}}) (1+\lambda_{i}T)^{-1}$$
 (3.1)

where:

 \bigwedge is the neutron generation time

 β_i is the importance weighted effective delayed neutron yield for the i^{th} group

 $\lambda_{\mathbf{i}}$ is the decay constant for the precursor of the \mathbf{i}^{th} group

 $\beta_{\mbox{\footnotesize eff}}$ is the effective delayed neutron fraction $T \mbox{ is the stable period of the reactor}$ $\rho_{\mbox{\footnotesize ex}}/\beta_{\mbox{\footnotesize eff}} \mbox{ is the excess reactivity in dollars.}$

Table 3.2 lists the values of the parameters used in the inhour equation as well as selected values of $\rho/\beta_{\mbox{eff}}$ and T for the four water-to-fuel ratios used.

^{26/} W. E. Schilling and D. H. Bryce, private communication (March, 1964).



80

90

100

TABLE 3.2 REACTIVITY PARAMETERS $\frac{a}{}$

W/F	1:1	2:1	3:1	4 - 1
β ₁ (%)	0.0397	0.0317	0.0310	0 0321
β ₂ (%)	0.2206	0.2125	0.2142	0 2147
β ₃ (%)	0.2023	0.1933	0.1942	0.1946
β4(%)	0.3553	0.3955	0,3945	0,3945
β ₅ (%)	0.1342	0.1229	0.1216	0 , 1207
β ₆ (%)	0.0480	0.0440	0.0437	0.0435
βeff ^(%) ,	0.7943	0.8630	0.8330	0.7955
$\lambda_1(\sec^{-1})$	0.0124	0.0124	0 .0124	0.0124
$\lambda_2(\sec^{-1})$	0.0305	0.0305	0.0305	0.0305
$\lambda_3(\sec^{-1})$	0.1111	0.1111	0.1111	0 . 1111
$\lambda_4(\sec^{-1})$	0.301	0.301	0.301	0,301
$\lambda_5(\sec^{-1})$	1.14	1.14	1.14	1.14
$\lambda_6(\sec^{-1})$	3.01	3.01	3.01	3.01
Λ/β _{eff} (sec) 0.004041	0.005411	0.007155	0.008976
	Reactivity (in	n \$) for period	T (in seconds)
T(sec)				
20 30 40 50 60 70	0.2889 0.2307 0.1937 0.1676 0.1480 0.1327	0.2799 0.2223 0.1859 0.1604 0.1414 0.1265	0.2812 0.2234 0.1868 0.1612 0.1421 0.1272	0.2819 0.2240 0.1874 0.1617 0.1425 0.1276

0.1146

0.1048

0.0967

0.1152

0.1054

0.0971

0.1156

0.1057

0.0974

0.1204

0.1102

0.1017

<u>a</u>/ S. S. Berg, footnote 1, pp. 157, 210, 232 (corrected by D. H. Bryce).



The difference in reactivity for two runs was divided by the difference in temperature to obtain values of the isothermal coefficient α . The average temperature $\overline{\theta}$ and the corresponding value of the volumetric coefficient of expansion of water $\overline{\beta}_{H_20}$ for the two runs were assigned to that value of α . $\overline{\beta}_{H_20}$ was determined by differencing a table of temperature dependent volumes of water $\overline{\beta}_{H_20}$. Figure B.1 is a plot of $\overline{\beta}_{H_20}$ vs θ . Tables B.1 - B.4 in Appendix B give the temperature, period, excess reactivity, and number of fuel rods for each run and for all water-to-fuel ratios. Values of α and $\overline{\beta}_{H_20}$ given in the same tables were used in another computer code to least squares fit the values of α to a linear function of $\overline{\beta}_{H_20}$

3.5 EXPERIMENTAL RESULTS

3.5.1 Temperature Dependent Excess Reactivity

Figures 3.1 through 3.4 show the temperature dependent excess reactivities of the cores investigated. Uncertainties in the values of ρ are within the size of the points of the graphs. Nominal water-to-fuel ratios are designated X:1-2 (read X to one dash two) where X is the water relative volume and the -2 indicates the core configuration. All the -2 cores were set up in the reactor with the removable unit cell at the

^{27/} C. D. Hodgman (Editor-in-Chief), <u>Handbook of Chemistry and Physics</u>, 42nd ed., p. 2143. Chemical Rubber Publishing Co., Cleveland, Ohio (1960).



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center of the lattice. As a result, all -2 cores are off center with respect to the reactor tank. A minimum distance of more than two feet separated the closest fuel rods from the grid plate support structure. The temperature dependent behavior of the reactor is not expected to be affected by the eccentricity of the core in the reactor tank.

3.5.2 <u>Isothermal Temperature Coefficient of Reactivity</u>

The isothermal reactivity coefficient for each of the four water-to-fuel ratios is shown in Figure 3.6 as a function of temperature and in Figure 3.7 as a function of the volumetric coefficient of expansion of water. Figures 3.8-3.11 give these values of α vs $\overline{\beta}_{H_2O}$ in greater detail for each core. The straight lines in Figures 3.7-3.11 represent the equation

$$\alpha = A + B \overline{\beta}_{H_2 0} \tag{3.2}$$

where A and B were determined by the method of least squares.

Fitted values of A and B are given in Table 3.3.

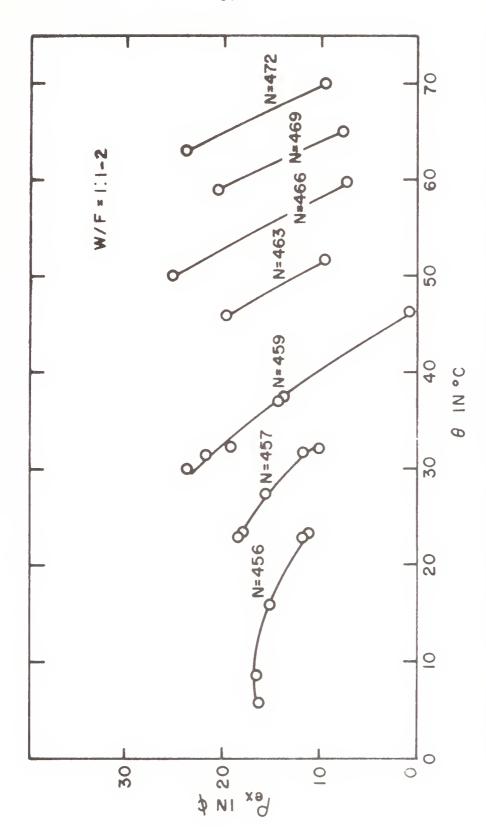
3.6 DISCUSSION OF RESULTS

3.6.1 Dissolved Air in the Water

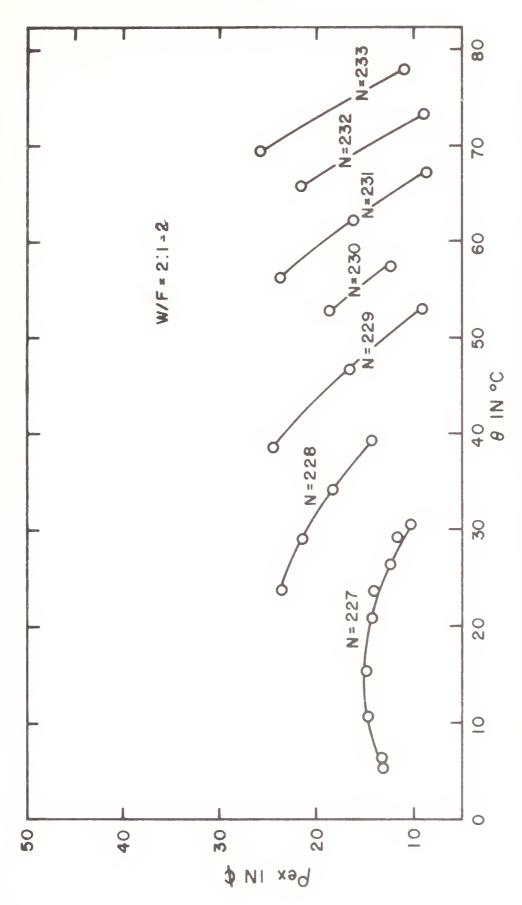
Some previous temperature coefficient work was plagued with the formation of air bubbles on the fuel rods $\frac{28.29}{}$

 $[\]frac{28}{}$ J. R. Brown, et al., footnote 4, p. 40.

^{29/} P. W. Davison, et al., footnote 5, p. 69.



Excess Reactivity vs Temperature for Various Fuel Rod Loadings, N. Figure 3.1:



Z Excess Reactivity vs Temperature for Various Fuel Rod Loadings Figure 3.2.

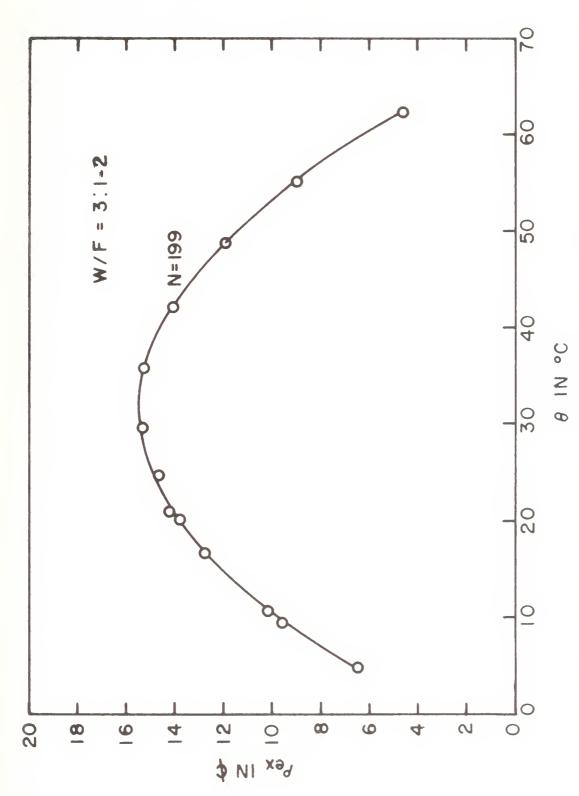


Figure 3.3: Excess Reactivity vs Temperature for a Fuel Rod Loading N = 199;



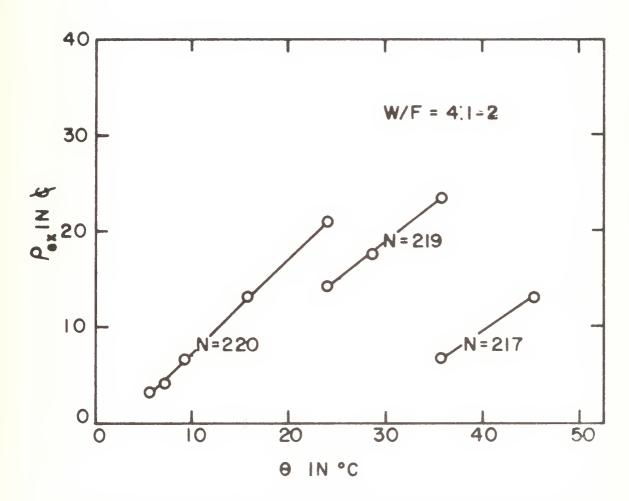
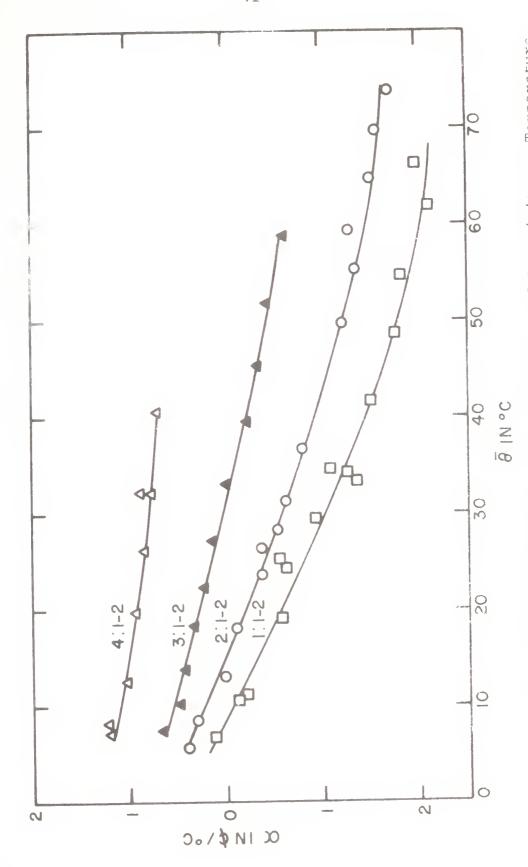


Figure 3.4: Excess Reactivity vs Temperature for Various Fuel Rod Loadings, N; 4:1-2.





isothermal Temperature Coefficient of Reactivity vs Temperature for Four Water-to-Fuel Ratios. Figure 3.5:

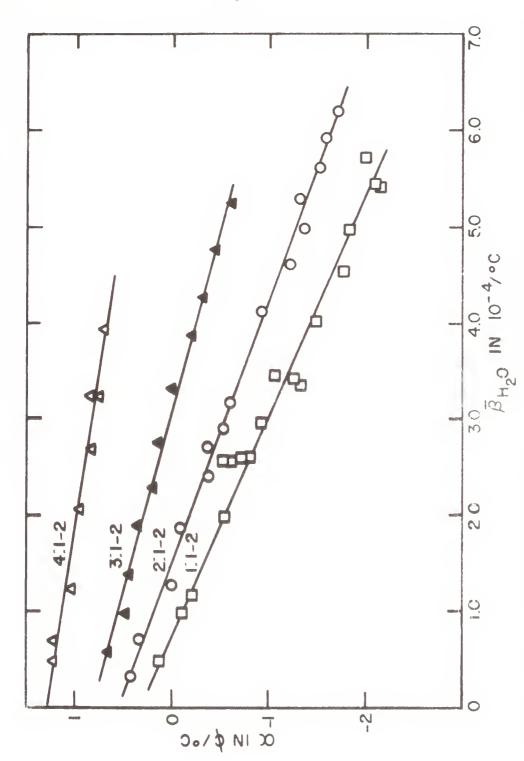


Figure 3.6: isothermal temperature Coefficient of Reactivity vs Volumetric Coefficient of Expansion of Water for Four Water-to-Fuel Ratios.

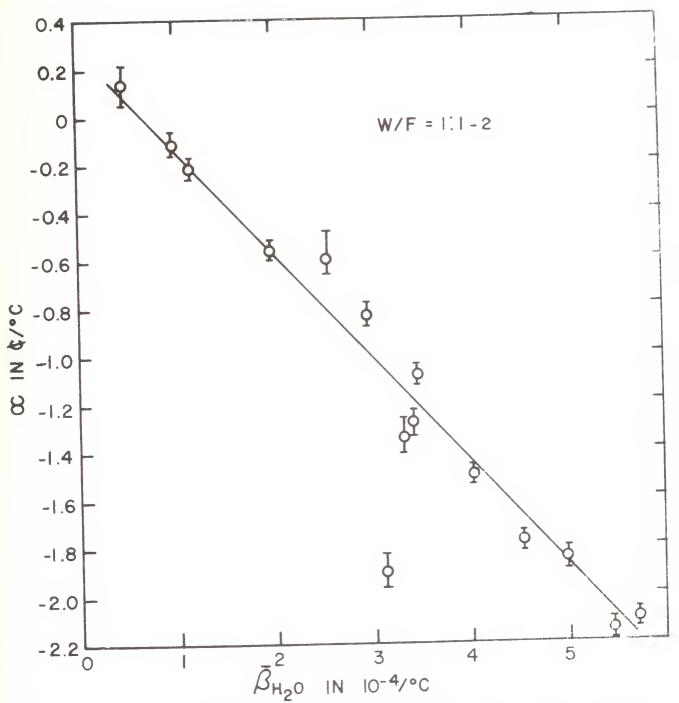


Figure 3.7: Isothermal Temperature Coefficient of Reactivity vs Volumetric Coefficient of Expansion of Water; 1:1-2.



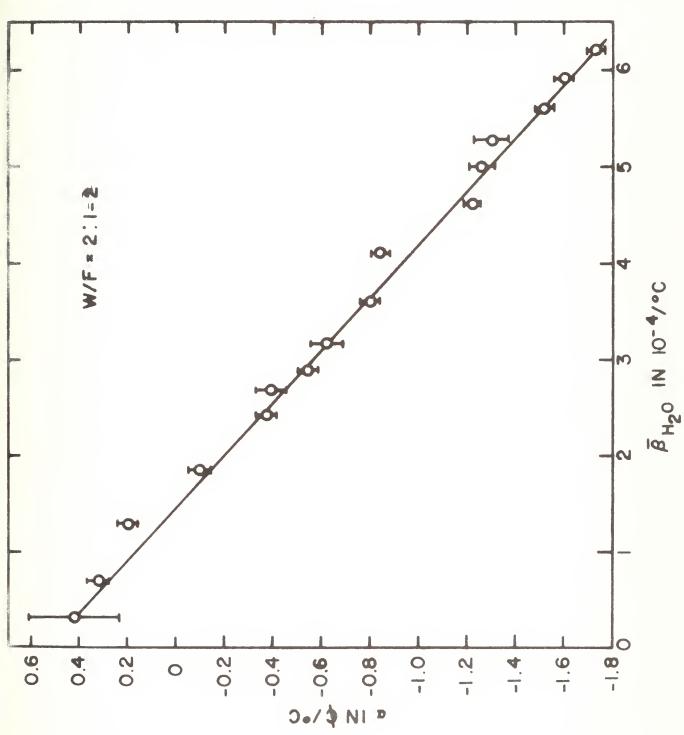
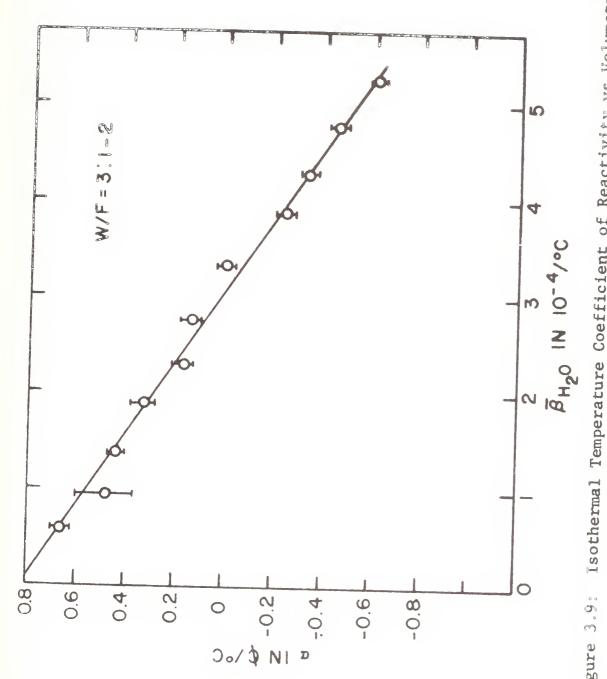


Figure 3.8: Isothermal Temperature Coefficient of Reactivity vs Volumetric Coefficient of Expansion of Water; 2:1-2.





Isothermal Temperature Coefficient of Reactivity vs Volumetric Coefficient of Expansion of Water; 3:1-2. Figure 3.9:

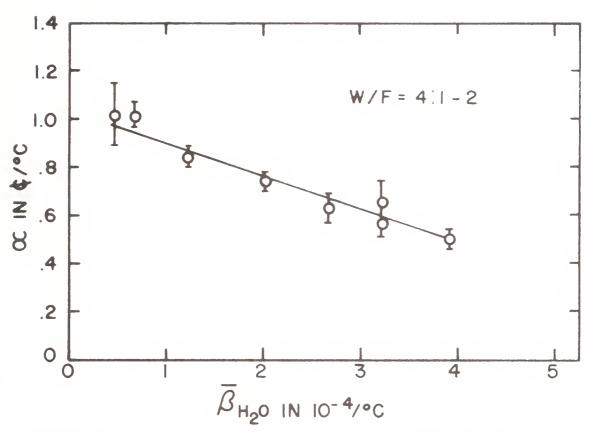
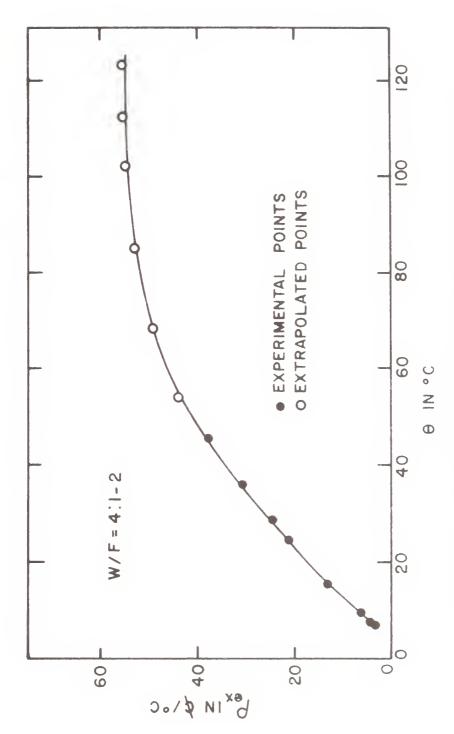


Figure 3.10: Isothermal Temperature Coefficient of Reactivity vs Volumetric Coefficient of Expansion of Water; 4:1-2.



Excess Reactivity vs Temperature; 4:1-2 Figure 3.11:

W/F	A(in ¢/°C)	B(in 10 ⁴ ¢)	Temperature Interval (°C)
1:1	0.29+0.02	-0.435+0.005	5 - 70
2:1	0.53+0.02	-0.367+0.006	5 - 78
3:1	0.82±0.02	-0.268+0.005	5 - 62
4:1	1.24+0.03	-0.138±0.011	7 - 45

These small air voids were thought to be responsible for some unexpected results in the measurement of the temperature coefficient. Two precautions were used by previous investigators. One was to use deaerated water to prevent the problem from arising. The other solution was to start at maximum temperature and cool the reactor. Air solubility being a maximum at low temperatures, by cooling the water from high temperatures no dissolved air would be released.

Two precautions were taken in the present experiment to prevent the formation of air bubbles on the fuel rods. First, the fuel rods were cleaned with acetone to remove grease and fingerprints which might tend to collect air bubbles. Second, water pumping was continued after the water level reached the



mouth of the overflow pipe leading back to the dump storage tank

The resulting circulation of water in the reactor tank tended to

flush away any air bubbles (and also speed up the approach to the

equilibrium temperature).

Systematic errors due to variation in dissolved air content of the water were estimated to be negligible. In the Cornell Zero Power Reactor, all water heating and cooling takes place external to the reactor tank. The only water temperature change occurring in the reactor tank is a small one (1°C or less) which is brought about by heating or cooling of the fuel rods and the reactor structure by the water as it is pumped into the reactor tank.

An agitator is installed in the dump storage tank to insure uniform properties of the water when pumped to the reactor tank. This mixing action aerates the water; therefore it was assumed that the water at each temperature was a saturated solution of air and water.

"Between the temperatures of 5°C and 8°C, the density of water saturated with air was found to be 0.000003_0 gm/ml less than the density of air-free water." At temperatures above this range, the solubility of air in water is less and therefore

^{30/} E. W. Washburn (Editor-in-Chief), <u>International Critical</u>

<u>Tables of Numerical Data, Physics, Chemistry and Technology</u>,

lst ed., p. 26. McGraw-Hill Book Company, Inc., New York

(1928).



the density effect is presumably even smaller. Density changes due to thermal expansion are large by comparison (of the order $10^{-4}/^{\circ}\text{C}$).

Under the assumption that dissolved air is added or removed in the dump storage tank, the change in solubility of air in the water results in a density change which is of no consequence for this experiment.

3.6.2 Temperature Dependent Excess Reactivity

The excess reactivity has been determined for four water-to-fuel ratios over the temperature intervals given in Table 3 3 Figures 3.1-3.4 give temperature-dependent excess reactivities for various fuel rod loadings with sufficient accuracy to plan further temperature dependence studies. Four thermocouples with a total worth of about -2¢ were in the lattices for these measurements.

For all water-to-fuel ratios, the excess reactivity curves have an initial positive slope. The temperature at which the maximum excess reactivity was observed was 8.8, 15.5, and 30.2 for the 1:1, 2:1, and 3:1 water-to-fuel ratios respectively. For the 4:1 core no maximum was reached; a curve of excess reactivity vs temperature for this core is shown in Figure 3.11. Experimental data are shown up to about 45°C; for higher temperatures the plotted points are from a linear extrapolation of α vs $\overline{\beta}$. For an increase in isothermal temperature from 20°C to 100°C, the reactivity added would be 35¢. Thus, for normal

room temperature operating conditions, a temperature increase to 100°C will not, in itself, lead to prompt criticality. Since the Safeguards Analysis $\frac{31}{}$ was based on the 4.1 core and assumed prompt criticality, there is no significant change in the analysis brought about by the determination of a positive isothermal temperature coefficient of reactivity for this core

3.6.3 Isothermal Temperature Coefficient of Reactivity

The isothermal temperature coefficient of reactivity has been measured for water-to-fuel ratios of 1:1, 2:1, 3:1, and 4:1 over temperature intervals listed in Table 3.3. The accuracy of the individual measurements of α is about 0.03-0.06¢/°C. The accuracy determined for α from the least squares fitted curve is 0.02¢/°C for three lattices, and 0.03¢/°C for the 4:1 lattice.

Within the accuracy of the measurements, A and B are different constants for each water-to-fuel ratio. Theoretical and experimental values of A and -B are plotted vs water-to-fuel ratio in Figure 3.12. The experimental curves shown merely connect the measured points smoothly and have no theoretical basis. However, they permit estimates by interpolation for the 1.5:1 water-to-fuel ratio: $A = 0.40 \pm 0.02$ in ϕ /°C and $B = -0.405\pm0.006$ in $10^4\phi$.

^{31/} S. S. Berg, "Final Safeguards Report to the U. S. Atomic Energy Commission for the Cornell University Zero Power Reactor," CURL-4, p. 7-3. Cornell University Reactor Laboratory (1962).



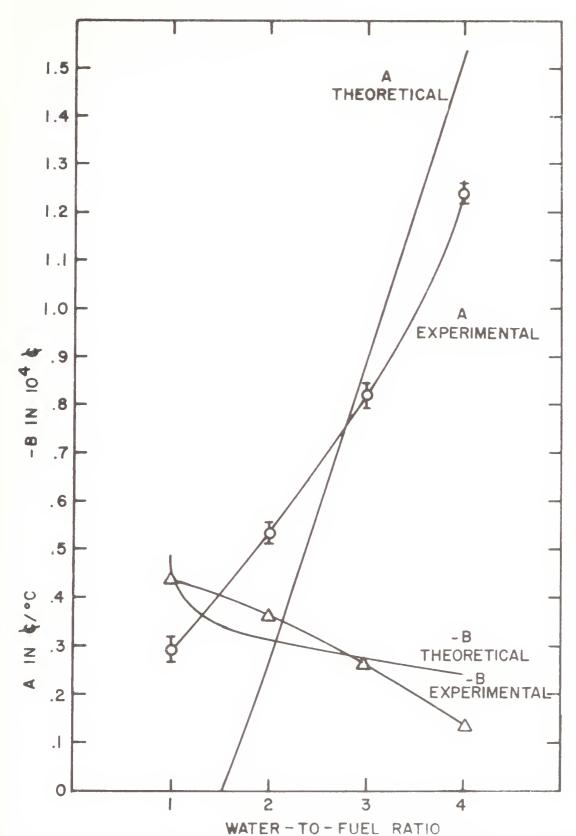


Figure 3.12: Theoretical and Experimental Value of A and D for the Equation $\alpha = A+B\overline{\beta}_{H_2}0$ as a Function. We we have the Fuel Ratio.

Theory predicts and experiment verifies a linear relationship between α and $\overline{\beta}_{H_20}$; however, Figure 3.12 shows disagreement between the measured and calculated values of A and B. This is a well-defined experiment. All parts of the reactor were at the same temperature. The control rods were fully withdrawn, and the fuel followers provided a clean core. For each temperature, a stable reactor period was measured. There were no large perturbations introduced by experimental devices. The experiment does not interfere with itself, as do flux measurements using foils. The conclusion therefore must be that the theory fails to predict the proper results, and further refinements in the calculations are necessary.

The only available previously published data which were complete enough and covered a large enough temperature range to permit useful plots of the isothermal temperature coefficient of reactivity as a function of temperature, and as a function of the volumetric coefficient of expansion of water, were for the SPERT-I reactor, a highly enriched pool reactor $\frac{32}{}$ The temperature range covered was 15-97°C. Figure 3.13 shows both α vs $\overline{\theta}$, and α vs $\overline{\beta}_{\rm H_2O}$ for the SPERT-I reactor. The temperature coefficient of reactivity is seen to be a linear function of the volumetric coefficient of expansion of water for this reactor also



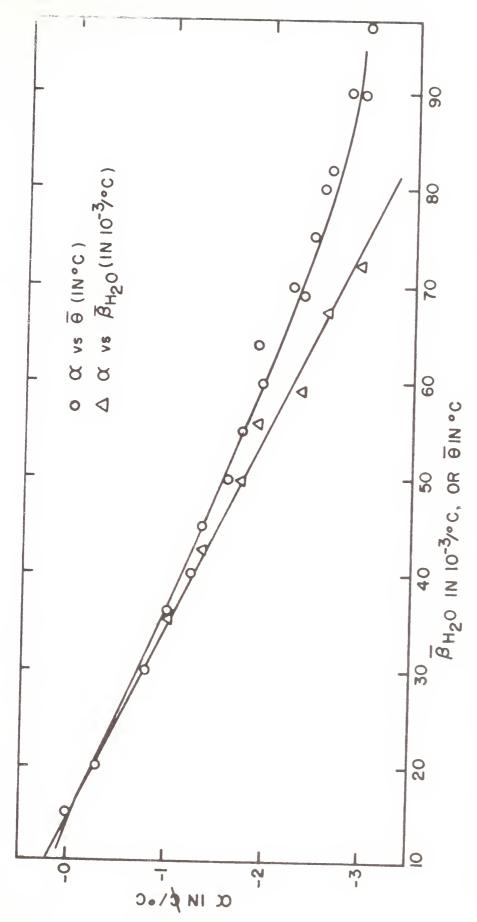


Figure 3.13: Isothermal Temperature Coefficient of Reactivity vs Volumetric Coefficient of Expansion of Water, and we Temperature for the SPERT-I Reactor.

Sec. 3.7

3.7 CONCLUSIONS

The excess reactivity has been measured as a function of temperature for water-to-fuel ratios of 1:1, 2:1, 3:1, and 4:1 with sufficient accuracy to allow planning of further temperature dependence experiments.

The isothermal temperature coefficient of reactivity has been measured for the same water-to-fuel ratios and was found to be a linear function of the volumetric coefficient of expansion of water for all lattices. Furthermore, the results of SPERT-I also exhibit this linearity of α vs $\overline{\beta}_{\rm H_2O}$. Theory disagrees with measured values of A and B, indicating a need for more sophisticated calculations for the isothermal temperature coefficient of reactivity.

CHAPTER 4

DISADVANTAGE FACTOR MEASUREMENT THEORY

4.1 THEORETICAL DISADVANTAGE FACTORS

Theoretical thermal disadvantage factors are calculated by taking ratios of spatially averaged thermal neutron densities, which include neutrons of all energies below the thermal neutron cutoff energy $\mathbf{E}_{\mathbf{c}}$ (or below the corresponding velocity $\mathbf{v}_{\mathbf{c}}$).

Honeck $\frac{33}{}$ gives the following definitions for the thermal neutron density, N(\underline{r}); thermal neutron density disadvantage factor, δ_n ; and the thermal flux disadvantage factor, δ_n :

$$N(\underline{r}) = \int_{0}^{v_{c}} N(\underline{r}, v) dv$$
 (4.1)

$$\delta_{n} = \frac{(1/V^{m}) \int d\underline{r} N^{m}(\underline{r})}{(1/V^{f}) \int d\underline{r} N^{f}(\underline{r})}$$

$$(4.2)$$

$$\delta_{n} = \overline{N}^{m}/\overline{N}^{f} \tag{4.3}$$

$$\delta_{\varphi} = \overline{\varphi}^{m}/\overline{\varphi}^{f} \tag{4.4}$$

$$\delta_{o} = \overline{v}^{m} \delta_{n} / \overline{v}^{f} \tag{4.5}$$

where

$$\overline{v} = \int_{0}^{V_{c}} vN(v) dv / \int_{0}^{V_{c}} N(v) dv$$
 (4.6)

 $[\]frac{33}{}$ H. C. Honeck, footnote 10, p. 50.



Sec. 4.1 - 4.2

in the fuel and moderator regions, and where:

r is the position vector;

 V^{m} , V^{f} are the moderator and fuel volumes;

 \overline{N}^m , \overline{N}^f are the spatially averaged thermal neutron densities in the moderator and fuel regions;

 $\overline{\phi}^m$, $\overline{\phi}^f$ are the spatially averaged total thermal fluxes in the moderator and fuel regions; and

 \overline{v}^m , \overline{v}^f are the velocities averaged according to Eq. (4.6) in the moderator and fuel regions.

MacVean 34/ used similar equations to calculate the thermal neutron densities, fluxes, average velocities, density disadvantage factors and flux disadvantage factors for the five water-to-fuel ratios of the Cornell University Zero Power Reactor. His results will be given later in this chapter as their use is required.

4.2 EXPERIMENTAL DISADVANTAGE FACTORS

The experimentally measured quantity $\delta_{\rm exp}$ which is related to the neutron density disadvantage factor is here called the dysprosium, manganese, or vanadium disadvantage factor depending on the foils used. This quantity is defined by

 $[\]frac{34}{}$ C. R. MacVean, footnote 2, pp. 143-145.

$$\delta_{\text{exp}} = \frac{\text{count rate per unit volume in the moderator foil}}{\text{count rate per unit volume in the fuel foil}}.$$
(4.7)

For a foil, the count rate per unit volume C is given by

$$C = e \text{ a s } (1/V) \text{ K(t)} \int d\underline{r} \int_{0}^{\infty} dE \ \Sigma_{\underline{a}}(E) \varphi(E,\underline{r})$$
(4.8)

where

e is the counter efficiency;

a is the foil self-absorption correction;

s is the foil self-shielding correction;

V is the foil volume (integration over \underline{r} is over the foil volume);

 $\Sigma_{a}(\mathbf{E})$ is the energy dependent activation cross section;

 $\phi(\textbf{E},\underline{\textbf{r}})$ is the energy and position dependent flux; and

K(t) is a time dependent function which takes into account the irradiation time, the time since reactor shutdown, and the counting time. For any given disadvantage factor measurement, K(t) will be the same for both moderator and fuel foils and will cancel out of the expression for the disadvantage factor. In practice it need not be calculated.

The counter efficiency, e, will be different for the differently shaped foils. This effect and an experimentally determined correction is discussed in the next chapter. For purposes of this chapter, e is assumed to cancel.

For small source-to-counter distances, the self-absorption factor, a, is a function of the source thickness only. 35/ Any sensitivity to geometric shape is determined experimentally and included in the counter efficiency correction factor discussed in the next chapter. For purposes of this chapter, then, the self-absorption factors will cancel in the expression for the disadvantage factor.

The self-shielding factor, s, may vary slightly from the fuel to moderator foils, but this variation is neglected for this work and the self-shielding factors are assumed to cancel in the expression for the disadvantage factor. Experimental determination of the self-shielding effect could be accomplished by measuring $\delta_{\rm exp}$ as a function of foil thickness and extrapolating to zero thickness.

If the energy range is broken up into the thermal region (E varying from 0 to E_c), and the fast region (E varying from E_c to ∞), the following expression can be written for a calculated value $\delta_{\rm calc}$ of the experimental quantity $\delta_{\rm exp}$:

^{35/} W. J. Price, <u>Nuclear Radiation Detection</u>, p. 132. McGraw-Hill Book Company, Inc., New York, Toronto, and London (1958).



$$\delta_{\text{calc}} = \frac{e \text{ as } K(t)(v^{m})^{-1} \int_{0}^{d\underline{r}} \int_{0}^{E_{c}} dE\Sigma_{\underline{a}}(E) \phi^{m}(E,\underline{r}) + \int_{E_{c}}^{\infty} dE\Sigma_{\underline{a}}(E) \phi^{m}(E,\underline{r})}{e \text{ as } K(t)(v^{f})^{-1} \int_{0}^{d\underline{r}} \int_{0}^{E_{c}} dE\Sigma_{\underline{a}}(E) \phi^{f}(E,\underline{r}) + \int_{0}^{\infty} dE\Sigma_{\underline{a}}(E) \phi^{f}(E,\underline{r})}{e \text{ as } K(t)(v^{f})^{-1} \int_{0}^{d\underline{r}} \int_{0}^{E_{c}} dE\Sigma_{\underline{a}}(E) \phi^{f}(E,\underline{r}) + \int_{0}^{\infty} dE\Sigma_{\underline{a}}(E) \phi^{f}(E,\underline{r})}{e \text{ (4.9)}}$$

On canceling e, a, s, K(t), and on using the following relation for the energy dependent, spatially averaged flux,

$$\overline{\varphi}(E) = V^{-1} \int d\underline{r} \varphi(E,\underline{r}) , \qquad (4.10)$$

Equation (4.9) can be written as

$$\delta_{\text{calc}} = \frac{\int_{0}^{E_{c}} dE \Sigma_{a}(E) \overline{\phi}^{m}(E) + \int_{E_{c}} dE \Sigma_{a}(E) \overline{\phi}^{m}(E)}{\int_{0}^{E_{c}} dE \Sigma_{a}(E) \overline{\phi}^{f}(E) + \int_{0}^{E_{c}} dE \Sigma_{a}(E) \overline{\phi}^{m}(E)} . \quad (4.11)$$

4.2.1 <u>1/v Thermal Cross Section Foils</u>

For a foil with a 1/v thermal activation cross section, $\Sigma_{\rm a}({\rm E})$ can be written

$$\Sigma_{a}(E) = \Sigma_{o} v_{o} / v \tag{4.12}$$

where the subscript o indicates a reference energy, and $\Sigma_{_{\hbox{\scriptsize o}}}v_{_{\hbox{\scriptsize o}}}$ is a constant. The calculated disadvantage factor then becomes

$$\delta_{\text{calc},1/v} = \frac{\int_{0}^{E_{c}} dE \Sigma_{o} v_{o} v^{-1} \overline{\phi}^{m}(E) + \int_{0}^{\infty} dE \Sigma_{a}(E) \overline{\phi}^{m}(E)}{\int_{0}^{E_{c}} dE \Sigma_{o} v_{o} v^{-1} \overline{\phi}^{f}(E) + \int_{E_{c}} dE \Sigma_{a}(E) \overline{\phi}^{f}(E)}.$$

$$(4.13)$$

Using the relations ϕ/v = N, ϕ = C_j/E for $E > E_c$ (where C_j is a constant), and

$$\int_{0}^{V_{C}} N(v) dv = \int_{0}^{E_{C}} N(E) dE, \qquad (4.14)$$

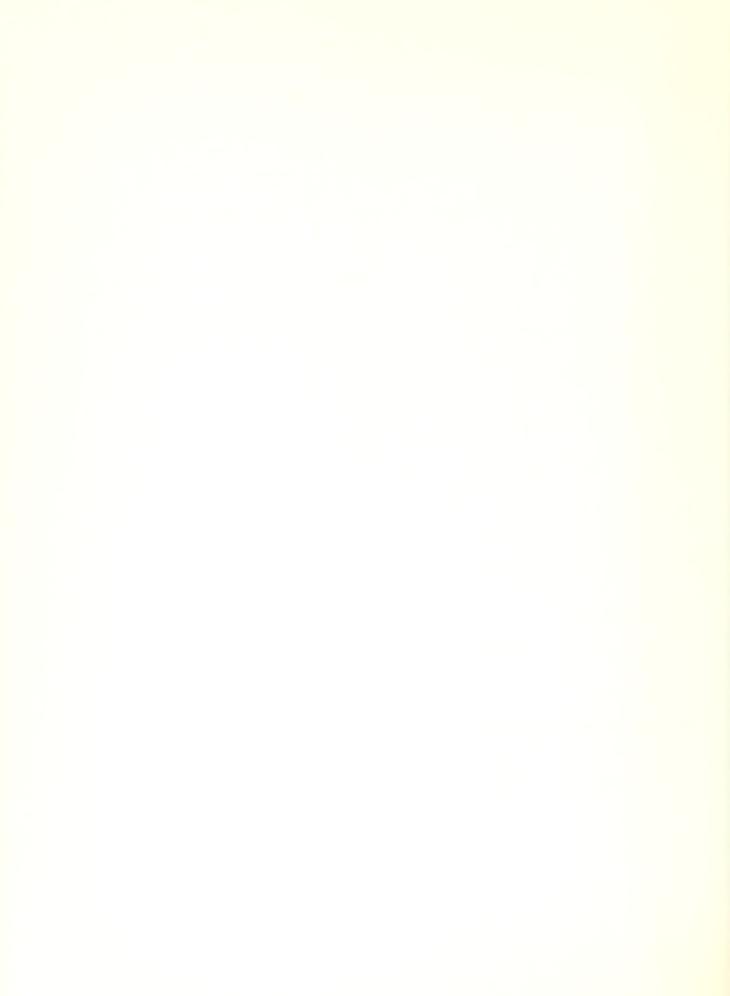
it follows that

$$\delta_{\text{calc},1/v} = \frac{\sum_{o} v_{o} \overline{N}^{m} + c_{j}^{m} \int_{E_{c}}^{\infty} dE \ E^{-1} \Sigma_{a}(E)}{\sum_{o} v_{o} \overline{N}^{f} + c_{j}^{f} \int_{E_{c}}^{\infty} dE \ E^{-1} \Sigma_{a}(E)} . \tag{4.15}$$

By simple manipulations it can be shown that

$$\delta_{\text{calc},1/v} = \delta_{n} \frac{1 + C_{j}^{m} RI/(v_{o}\sigma_{o}\overline{N}^{m})}{1 + C_{j}^{f} RI/(v_{o}\sigma_{o}\overline{N}^{f})}$$

$$= \delta_{n}W$$
(4.16)



where

 δ_n is defined by Eq. (4.3); $C_{\mathbf{j}}^{m}$, $C_{\mathbf{j}}^{f}$ are the epithermal flux proportionality constants; W is defined by the expression in the brackets; RI is the infinite-dilution resonance integral for the foil;

 v_{o} is the thermal reference velocity (2200 m/sec); and σ_{o} is the activation cross section of the foil at the energy corresponding to v_{o} .

If the second term in both the denominator and numerator of Eq. (4.16) were small compared to 1, $\delta_{\rm calc,1/v}$ would be equal to $\delta_{\rm n}$.

The resonance integral for the foil is defined by

$$RI = \int_{E_{C}}^{\infty} E^{-1} \sigma_{a}(E) dE . \qquad (4.17)$$

For the experimental values of RI used in the present calculations, \mathbf{E}_c was 0.4 eV. However, the values of $\overline{\mathbf{N}},~\delta_n,$ and δ_ϕ calculated by MacVean are for a cutoff energy of 1.6 eV. Corrections for the different values of \mathbf{E}_c were made according to the following scheme.

Let $\overline{N}_{1.6}$ be given by

$$\overline{N}_{1.6} = \int_{0}^{1.6} dE \ \overline{N}(E) . \tag{4.18}$$

A similar expression defines $\overline{N}_{0.4}$. Then

$$\overline{N}_{0.4} = \overline{N}_{1.6} - \int_{0.4}^{1.6} dE \ \overline{N}(E)$$
 (4.19)

In the region $0.4 \le E \le 1.6$, let

$$\overline{N}(E) = \varphi(E)/v(E)$$

$$= C_{j}E^{-1}v(E)^{-1}$$
(4.20)

where C_j is selected to be that value given by $E\varphi(E)$ from the COUTH spectra $\frac{36}{}$ at 0.55 eV. For v(E) in m/sec, and E in eV, the relationship between v and E can be written

$$0.723 \times 10^{-6} \text{ v(E)} = \text{E}^{1/2}$$
 (4.21)

Using Eqs. (4.20) and (4.21), $\overline{\mathrm{N}}_{0.4}$ is seen to be

$$\overline{N}_{0.4} = \overline{N}_{1.6} - 1.142 \times 10^{-6} C_i$$
 (4.22)

where \overline{N} is in n/cm^3 and C_i is in n/cm^2 -sec.

Table 4.1 gives the values of $\sigma_{\rm o},\ {\rm v_o},\ {\rm and}\ {\rm RI}$ for the three foil materials used.

Values of W, C $_{\rm j}$, $\overline{\rm N}_{0.4},$ and the calculated $^{\delta}{\rm calc},1/v$ are listed in Table 4.2 for the foils used.

4.2.2 Foils with a Non-1/v Thermal Cross Section

For a foil whose thermal cross section deviates from 1/v, $\delta_{\rm calc}$ can be computed from Eq. (4.11) by integrating the energy dependent cross sections over the spectra of the fuel



TABLE 4.1 RESONANCE INTEGRALS AND 2200 M/SEC CROSS SECTIONS FOR ${\rm Dy}^{164}$, Mn, and V

_{Dy} 164	Mn	V	
482 <u>a</u> /	14.3 ^b /	2 <u>b</u> /	
2600 <u>c</u> /	13.4 <u>c</u> /	4.5 ^c /	
	482 <u>a</u> /	482 <u>a</u> / 14.3 <u>b</u> /	$482\frac{a}{}$ $14.3\frac{b}{}$ $2\frac{b}{}$

- a/ J. L. Crandall in "Reactor Physics Constants," 2nd ed. (L. J. Templin, ed.) ANL-5800, p. 164, Argonne National Laboratory (1963).
- b/ D. J. Hughes, <u>Pile Neutron Research</u>, p. 139. Addison-Wesley Publishing Co., Inc., Cambridge, Mass., 1953.
- <u>c</u>/ D. J. Hughes and J. A. Harvey, "Neutron Cross Sections," BNL-325, pp. 7-18, Brookhaven National Laboratory (1955).



TABLE 4.2 THERMAL PARAMETERS FOR CALCULATING DISADVANTAGE FACTORS AT 20 $^{\circ}\text{C}$ FOR $1/\nu$ THERMAL CROSS SECTIONS

W/F	1:1	2:1	3:1		
	mod fuel	mod fuel	mod fuel		
$C_j = \frac{a}{(n/cm^2 - sec)}$.7993 .7708	.8274 .7955	.8371 .8028		
$\overline{N}_{1.6} \stackrel{b}{=} (in 10^{-6} n/cm^3)$	14.58 11.65	28.62 21.18	41.50 29.19		
$\overline{N}_{0.4} \stackrel{c}{=} (in 10^{-6} n/cm^3)$	13.67 10.77	27.68 20.27	40.54 28.27		
⁵ n,0.4	1.269	1.366	1.434		
W_{Dy}	0.990	0.992	0.993		
⁶ Dy,1/v	1.256	1.355	1.424		
W_{Mn}	0.953	0.962	0.967		
[∂] Mn,1/v	1.209	1.314	1.387		
$W^{\mathbf{V}}$	0.976	0.982	0.986		
δ v, 1/v	1.238	1.341	1.414		

 $[\]underline{a}$ / $C_j = E\varphi(E)$ @ 0.55 eV from COUTH Spectra: C. R. MacVean, footnote 2, pp. 136-139.

 $[\]frac{b}{}$ W. E. Schilling, private communication (August, 1964). $\frac{c}{}$ Calculated from Eq. (4.22).

and moderator. The expression for $\delta_{\rm calc}$ can be simplified somewhat by defining appropriate average cross sections and utilizing the resonance integral information above.

The spatially averaged total thermal neutron flux for both the moderator and fuel regions is given by

$$\overline{\varphi} = \int_{0}^{E_{c}} \overline{\varphi}(E) dE . \qquad (4.17)$$

Average thermal cross sections are defined by

$$\overline{\sigma}_{a} = \int_{0}^{E_{c}} dE \sigma_{a}(E) \overline{\phi}(E) \int_{0}^{E_{c}} dE \overline{\phi}(E)$$
 (4.18)

where $\overline{\sigma}$ for the moderator and fuel regions are integrated over the respective spectra.

It can be shown that application of the above expressions gives for $\delta_{\mbox{\footnotesize calc}}$

$$\delta_{\text{calc}} = \delta_{\phi} \frac{\overline{\sigma_{a}^{m}}}{\overline{\sigma_{a}^{f}}} \left[\frac{1 + C_{j}^{m} RI/(\overline{\sigma_{a}^{m}} \overline{\phi}^{m})}{1 + C_{j}^{f} RI/(\overline{\sigma_{a}^{f}} \overline{\phi}^{f})} \right]$$

$$= \delta_{\phi} (\overline{\sigma_{a}^{m}}/\overline{\sigma_{a}^{f}}) X \qquad (4.19)$$

where X is defined by the expression in brackets. For a 1/v thermal absorber,



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$$\frac{\sigma_{a}}{\sigma_{a}} = \int_{0}^{E_{c}} dE \sigma_{o} v_{o} \phi(E) v^{-1} / \int_{0}^{E_{c}} dE \phi(E)$$

$$= \sigma_{o} v_{o} / \overline{v} \tag{4.20}$$

and Eq. (4.19) reduces to Eq. (4.16) as it should.

Both manganese and vanadium thermal activation cross sections are very nearly 1/v. The thermal activation cross section for dysprosium, however, does vary from 1/v. The dysprosium cross sections were taken from Sher, et al. $\frac{37}{}$ These dysprosium cross sections and 1/v cross sections for manganese and vanadium were averaged over the COUTH spectra for water-to-fuel ratios of 1:1, 2:1, and 3:1. The values of these averaged cross sections, values of X, $\overline{\phi}_{0.4}$ (total thermal flux for a cutoff energy 0.4 eV), and the various disadvantage factors are given in Table 4.3.

4.3 TEMPERATURE DEPENDENCE OF THE DISADVANTAGE FACTOR

MacVean calculated the thermal neutron density and flux disadvantage factors according to the equations of Section 4.1. By calculating these thermal properties of

 $[\]frac{37}{}$ R. Sher, et al., "Low Energy Cross Sections of Dy 164 ," Nuc. Sci. Eng. $\underline{11}$, 369-376 (1961).

TABLE 4.3 $\label{thermal_parameters} \mbox{ Thermal parameters for calculating disadvantage factors at 20°C } \mbox{ for non-1/v Thermal cross sections}$

W/F		:1	2:1		3:1	
	mod	fuel	mod	fuel	mod	fuel
$\overline{N}_{1.6} \stackrel{a}{=} (n/cm^3)$	14.58	11.65	28.62	21.18	41.50	29.19
1.0	3667		3134	3446	2945	3265
$\overline{\varphi}_{1.6} (n/cm^2-sec)$			8.9695	7.2986	12.2218	9.5305
$C_j = \frac{a}{(n/cm^2 - sec)}$	0.7993	0.7708	0.8274	0.7955	0.8371	0.8028
a, Dy	1735		1937	1765	2019	1820
$\sigma_{a,Mn} = \frac{a}{\sqrt{a}}$ (barns)	9.300	8.733		9.452		9.711
$\overline{\sigma}_{a,V} \stackrel{a/}{=} \text{(barns)}$	3.507	3.295	3.856	3.566	3.999	3.664
$\overline{\varphi}_{0.4}$ (n/cm ² -sec)	4.2764	3.5943	7.8618	6.2336	11.1011	8.4558
δφ,0.4	1.	190	1.2	261	1.3	313
X _{Dy}	0.9	989	0.9	991	0.9	993
δ _{Dy}	1.	269	1.3	371	1.4	446
X_{Mn}	0.9	953	0.9	961	0.9	967
δ _{Mn}	1.3	208	1.3	310	1.3	386
x_{V}	0.9	980	0.9	983	0.9	987
δ _V	1.3	241	1.3	340	1.4	14

 $[\]underline{a}$ / W. E. Schilling, private communication (August, 1964).

 $[\]frac{b}{}$ C. R. MacVean, footnote 2, p. 141.



the reactor at two different temperatures (20° and 40°C), the temperature dependent behavior of these properties was predicted. Table 4.4 gives the calculated values of the neutron density disadvantage factor at 20°C, the logarithmic slope $(1/\delta_n)(d\delta_n/d\theta)$, and the slope $d\delta_n/d\theta$.

TABLE 4.4 TEMPERATURE DEPENDENCE OF δ_n

W/F	δ _n <u>a</u> /	$(1/\delta_n)(d\delta_n/d\theta)^{a/2}$ in $10^{-4}/^{\circ}C$	do _n /d⊖ in 10 ⁻⁴ /°C
1:1	1.252	-2.76	-3.46
2:1	1.351	-4.46	-6.02
3:1	1.422	-5.56	-7.91

 $[\]underline{a}$ / C. R. MacVean, footnote 2, pp. 141-143.

CHAPTER 5

EXPERIMENTAL METHODS AND RESULTS FOR THERMAL DISADVANTAGE FACTORS

5.1 REACTOR DESCRIPTION

5.1.1 The Unit Cell

The lattices of the Cornell University Zero Power
Reactor consist of an upper fuel rod support grid plate,
a lower fuel rod positioning grid plate, structural support
members, the reactor tank, the fuel rods, and four control
rod units each containing a cluster of three control elements in an equilateral triangle of the same pitch as the
rest of the core. These control rod clusters may be
positioned in any location of the reactor because the
control elements have the same outside diameter as a normal
fuel rod. The upper portion of each control element contains the boron carbide poison. The lower portion is a fuel
follower with the same dimensions as the normal fuel rods.

The upper grid plate has an insert which allows the removal or insertion of four fuel rods as a unit in what is called the unit cell. These four fuel rods form a parallelogram of two equilateral triangles of the lattice pitch. For all water-to-fuel ratios, the unit cell is slightly off-center with respect to the upper grid plate and the reactor tank. All cores studied were assembled

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with the unit cell at the center of the fuel loading to reduce the radial flux gradient in the unit cell. With a triangular (or hexagonal) lattice, one fuel rod must be the exact center of the core. Therefore, of the four fuel rods of the unit cell, one was the central element of the reactor and the other three were in the first hexagon out.

5.1.2 Activation Rods

The original design of the reactor facility included decappable fuel rods for the purpose of introducing foils into the fuel region of the reactor. These rods were slightly longer than the normal fuel rods but contained a normal 48-inch fuel loading.

Because the full-length decappable fuel rod is too long to fit into the hood used for handling radioactive materials, and because it is difficult to insert and remove foils with this length of fuel rod, a special "activation" rod was designed. The eighteen-inch fuel section of the activation rod is supported by screw-in aluminum rods which make this special rod the same over-all length as a standard fuel element. (See Figure 5.1) When detached, the fuel section is short enough to be handled easily in the hood. It is easy to insert and remove foils with this rod because only a few fuel pellets need be handled. Because of the small size, ease in handling, and small number of fuel pellets handled, experiments can be accomplished with less radiation exposure to personnel than was previously possible with the longer rods.

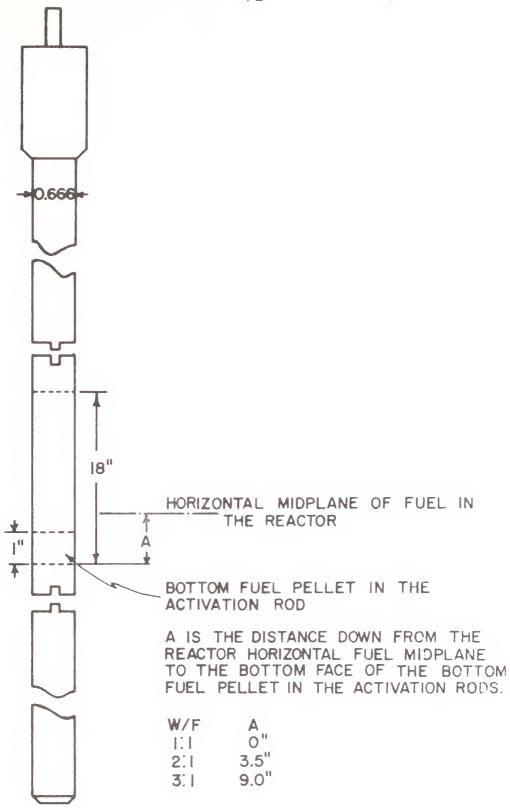


Figure 5.1: The Activation Rod.

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The activation rods are used for foil and wire activation within the fuel region of the core. They can be placed in any normal fuel rod position, but for the disadvantage factor work they were used only in the unit cell. The four fuel rod positions of the unit cell were filled with three activation rods and one normal fuel rod. The standard loading was as shown in Figure 5.2.

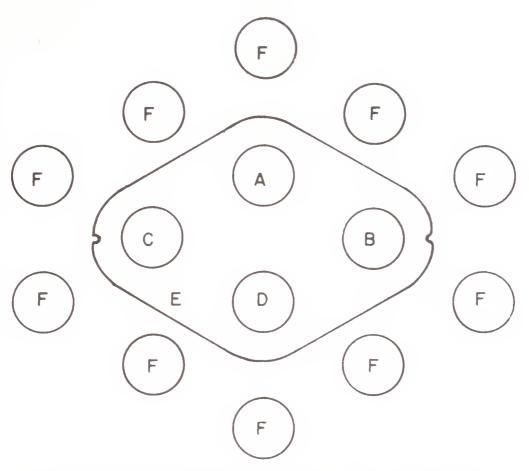
5.2 FOIL PREPARATION

5.2.1 Foil Types and Manufacture

The foils used for the disadvantage factor measurement were five mil-thick dysprosium, manganese, and vanadium. The dysprosium was obtained from General Astrometals Corporation and consisted of 5.24% dysprosium in aluminum. The manganese was in the form of an alloy called P-metal which is about 72% manganese, 18% copper, and 10% nickel. The P-metal was obtained from Metals and Controls, Inc., and has a thickness tolerance of ± 0.00025 inch. The vanadium was obtained from H. Cross Co.

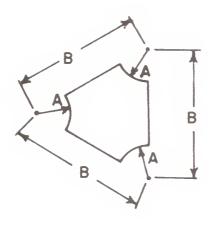
The fuel region foils were punched from stock with a 0.600 ± 0.001 -inch diameter die. Moderator region foils were punched from stock using a machined die of appropriate shape. Figure 5.3 shows the dimensions and shape of the moderator foils.





- A ACTIVATION ROD IN CENTRAL FUEL POSITION OF THE UNIT CELL.
- B,C ACTIVATION RODS IN FIRST HEXAGON POSITIONS OF THE UNIT CELL.
- D NORMAL FUEL ELEMENT IN A FIRST HEXAGON POSITION OF THE UNIT CELL.
- E REMOVABLE UNIT CELL FUEL ROD SUPPORT PLATE.
- F NORMAL FUEL RODS IN NORMAL LATTICE POSITION.

Figure 5.2: Top View of the Unit Cell.



W/F	A	В
	(in)	(in)
1:1	0.675	0.856
2:1	0.675	1.030
3:1	0.675	1.177

Figure 5.3: Moderator Foil Dimensions.

5.2.2 Foil Placement in the Reactor

To prevent fission product contamination of the fuel foils, a special fuel pellet with an aluminum foil glued to one end with G.E. Glyptal was placed on each side of the fuel foils. See Figure 5.4. Ten fuel pellets were removed from the activation rod and an aluminum lined fuel pellet was inserted. The manganese fuel foil was placed next to the fuel pellet liner. Pellet and foil were pushed to full insertion with a lucite rod which was marked for transferring the foil position to the outside of the activation Another lined pellet was inserted, followed by a normal fuel pellet. This loading sequence was continued for dysprosium and vanadium foils until each activation rod had a manganese foil at the center of the rod, a dysprosium foil three inches below the center of the rod, and a vanadium foil another three inches lower. Figure 5.1 gives the distance between the horizontal midplane of the fuel in the reactor and the bottom edge of the bottom fuel pellet in the activation rod for the three water-to-fuel ratios studied.

Two moderator foils were secured to a one-eighth-inch thick lucite moderator support plate with double-backed Scotch tape. The unit cell was assembled with three activation rods and a normal fuel rod. Using the marked lucite fuel foil insertion rod, the lucite moderator foil supports were positioned at the proper levels on the outside of the



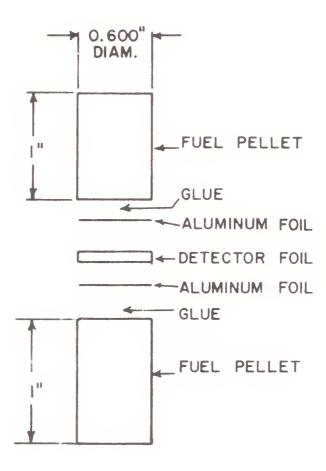


Figure 5.4: Fuel Foil Placement in the Activation Rod.

activation rods. The assembly was taped together with Band Aid Air Vent adhesive tape placed about three inches above the manganese foils and about three inches lower than the vanadium foils. (This tape was found to be easy to use, to keep its adhesive properties under water, and to come cleanly off the fuel rods leaving no sticky residue.) To insure positive positioning of the lucite moderator support plates, and to prevent loss of foils, waxed string was looped around the fuel rods immediately above and below the support unit. Figure 5.5 shows the assembly ready for insertion into the reactor.

The assembled unit cell was then loaded into the reactor and irradiated for a period of about ten to twenty minutes at flux levels corresponding to about one-half watt in power. Irradiation times and power levels were adjusted to give good count rates with minimum personnel exposure during handling of the fuel.

It was necessary to remove the unit cell assembly as rapidly as possible to get any information at all from the short-lived vanadium foils (half life of 3.8 minutes).

After a wait of about five minutes from shutdown, the activation rods were removed to the radioactive handling hood for disassembly. The vanadium foils were removed, washed in acetone, and beta-counted on an automatic sample changer. About one hour after shutdown, the manganese and dysprosium



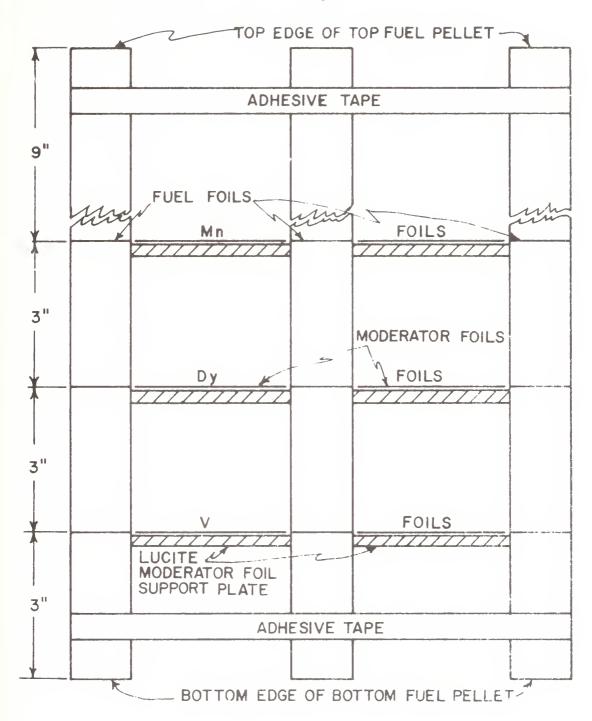


Figure 5.5: The Unit Cell Foil Assembly.

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foils were removed from the fuel, washed in acetone, and counted on the automatic sample changer.

5.3 COUNTING TECHNIQUES -- SOLID FOILS

5.3.1 The Automatic Counter System

The automatic counting system described by Rushing 38/ and Berg 39/ was used for the solid foil counting. There are 24 sample positions on a round table which pneumatically advances on electronic signal. The samples are held on pedestals which are pushed up next to a thin-window proportional flow counter for counting. The timing interval, table rotation, two scalers, and a printer are controlled electronically.

Uniform counting geometry for the fuel foils was provided by pedestals which were machined to accept 0.600-inch foils. The moderator foils were centered by eye on similar pedestals.

5.3.2 Relative Fuel and Moderator Foil Counter Efficiencies

Counter efficiency is slightly sensitive to distance from the center of the pedestal. $\frac{40}{}$ Therefore an experi-

^{38/} J. C. Rushing, "Report of Work Done on an Automatic Sample Changer for Use in the Cornell University Nuclear Reactor Laboratory," Department of Engineering Physics Senior Project (1962).

 $[\]frac{39}{}$ S. S. Berg, footnote 1, pp. 101-107.

mental geometric correction factor was determined for this effect as follows. Fuel and moderator foils were irradiated on a flux wheel in the uniform thermal flux of the TRIGA hohlraum 41/ and both shapes were counted on the automatic counting system. After irradiation in a uniform flux, the two shapes of foils should have the same activation per unit volume. The foils were counted using the Geneva motion described in Section 5.3.4. The ratio of fuel foil count rate per unit volume to the moderator foil count rate per unit volume is the desired geometrical correction factor. These correction factors are given in Table 5.1 for the three water-to-fuel ratios studied.

TABLE 5.1

EXPERIMENTALLY DETERMINED COUNTER EFFICIENCY CORRECTION FACTORS

W/F	1:1	2:1	3:1
Factor <u>a</u> /	0.990	1.007	1.014

 $[\]frac{a}{}$ The statistical error is about 0.004 for all factors.

^{40/} E. B. Fehr, internal memo RM-16, Cornell University
Nuclear Reactor Laboratory (1964).

^{41/} E. B. Fehr and E. P. Whitted, internal memo RM-15, Cornell University Reactor Laboratory (1964).



5.3.3 Data Reduction for Vanadium Foils

The short half-life of the vanadium foils made it necessary to analyze the data differently than the data from the other two foils. The vanadium foils were counted in a given order on both proportional counters of the automatic counting system. The count rate at the start of counting was about 1,000 counts per second. The foils were counted down to about 20 counts per second. SAT I, $\frac{42}{}$ a local computer code, was used to correct each datum point back to the activity on removal from the reactor. These count rates on removal were then converted to count rate per unit volume. The moderator foil count rates were averaged, as were the fuel foil count rates. The ratio of these averaged count rates per unit volume for the moderator and fuel foils was corrected by the appropriate geometrical correction factor of Table 5.1; the result was the desired vanadium disadvantage factor δ_V .

5.3.4 Data Reduction for Manganese and Dysprosium Foils

Manganese and dysprosium have half-lives of 2.59 hours and 2.42 hours respectively. This is sufficiently long to allow use of the Geneva motion counting technique. In this method, the foils are counted in a given order once through. The last foil is counted twice. The remaining foils are then counted in the reversed order. For a total counting time

^{42/} W. E. Schilling, internal memo, Cornell University Reactor Laboratory (1962).



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sufficiently short compared with the half-life of the foils, a simple arithmetic time average of two counts is very close to the actual counts at the midpoint in time. For example, for a total counting time of 20 minutes, the arithmetic average of the end point counts is within 0.3% of the true counts at the midpoint time. The total counting time was usually about 10 minutes; therefore the error is even less. Statistical accuracy of counting was generally of the order 0.7% and thus the error introduced by using the Geneva counting method is much less than the statistical error.

5.4 COUNTING TECHNIQUE -- DISSOLVED FOILS

The manganese foils were counted with a "soluble" method in which the foils were dissolved in acid and aliquots of the solution were gamma-counted in a well-type scintillation counter. Counting of aliquots of solutions of foils provides two advantages over solid foil counting. First, the moderator and fuel foils are counted under identical counting geometry. Thus, there is no need to determine a counter efficiency correction factor. Second, the process of dissolving the foil averages the count rate of the foil over its volume. The count rate of the aliquot is then directly proportional to the total count rate of the foil itself, the constant of proportionality being the fraction of the total solution which is being counted. For both moderator and fuel foils,

the constant of proportionality was the same. The above total count rate, when divided by the volume of the foil, is exactly the spatially averaged count rate per unit volume needed to determine the manganese disadvantage factor.

5.4.1 Foil Preparation

After the solid foils had been counted as described in Section 5.3.4, they were removed to the fume hood in the isotope handling room. Each foil was cut with metal shears so that it would fit down the neck of a ten-milliter volumetric flask into which about five milliliters of 3N HNO₃ had previously been placed. Once the foil was dissolved, the solution was diluted to 10 milliliters with distilled water. Each solution was then mixed well.

Three milliliters of the solution were pipetted off and placed into a plastic vial, and the vial was capped. Each foil had its own vial; each vial had three milliliters of solution. Two pipettes were used, one for the fuel foils and one for the moderator foils to prevent mixing in the pipette of solutions with different activities.

5.4.2 Counting of the Solutions

The vials fit snugly into the well of the scintillation counter, the top surface of the solution being below the top of the crystal. The geometrical arrangement in the counter was identical for each solution.



Three counting methods were initially investigated. First, a multichannel analyzer was used to get the gamma spectrum of the solutions. The area under the peak was determined by numerical integration. These total counts were divided by the foil weight to get counts per unit weight, and the ratio of the average counts per unit weight for moderator and fuel foils gave the experimental disadvantage factor.

The second method was to count the solution on a single channel analyzer in the differential mode, adjusting the base line and window width to straddle the gamma peak.

Again, the ratio of counts per unit weight for moderator and fuel foils was the desired disadvantage factor.

The third method used an integral discriminator with the base line in the valley above the Compton edge. In this manner, all counts above the base line were included in the count rate per unit weight.

All three methods gave the same result within experimental error. The third method was chosen because of simplicity of analysis, greater availability of the associated electronic equipment, and higher count rate which resulted in greater statistical accuracy.

The aliquots were counted using the Geneva motion previously described. Typical counting times were one minute per vial; typical total counts were of the order 50,000. The background counts were subtracted from the total counts



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prior to averaging the counts per unit weight for the fuel and moderator foils. A typical data reduction is given in Table 5.2.

5.5 EXPERIMENTAL RESULTS

Disadvantage factors were measured as previously described at various temperatures for three water-to-fuel ratios. The experimental results are given in Table 5.3 as δ_{Dy} , δ_{Mn} , δ_{Mn} , δ_{Mn} , δ_{Mn} , and δ_{V} . All values except the dissolved foil experiment have been corrected for geometry by the correction factors of Table 5.1. Soluble manganese experiments had identical counting geometry and therefore needed no geometric correction factor.

Values for the disadvantage factors from Table 5.3 were least-squares fitted to a linear function of temperature. Table 5.4 gives fitted experimental values and theoretical values of the disadvantage factors at 20°C. Both experimental and theoretical values of the slope of the δ vs θ curves are also given.

Temperature dependent values of $\delta_{\rm Mn}$ and $\delta_{\rm Mn,sol}$ are plotted in Figure 5.6 for the three water-to-fuel ratios investigated. Figure 5.7 gives $\delta_{\rm Dy}$ vs temperature for the 3:1-2 core. Figure 5.8 gives $\delta_{\rm V}$ vs temperature for the same core.



TABLE 5.2

DATA ANALYSIS FOR A TYPICAL MANGANESE DISADVANTAGE FACTOR

USING DISSOLVED FOIL TECHNIQUE MEASUREMENT

Single Channel Analyzer Settings, Integral Mode

01	ingic one	IIIICI AIIC	ilyzer be	ccings, inc	cgrai noc	
Fine Ga	ain ().5		Base Li	ne 17	.0 V
Coarse	Gain 4	+		Window	Width 0	. 5V
Clippir	ng Time ().5 (micr	oseconds) Discrim	ninator 8	5.5 V
Foil ^a / Number		per	Weight/	Average Counts/ Weight, Moderator Foils		^δ Mn,Sol
119 307 124 317 131 131 317 124 307 119	0.1748 0.2534	21402 39897 21043 40677 21373 20629 39083 20774 38564 20527	239 273	310 868	238 376	1.304± 0.007

Foils numbered in the 100's are fuel foils; those in the 300's are moderator foils. These foils are for the 3:1 core.

 $[\]frac{b}{}$ Counts per unit weight per minute are the sum of counts for each foil, corrected for background of 176 counts per minute, and divided by the foil weight.

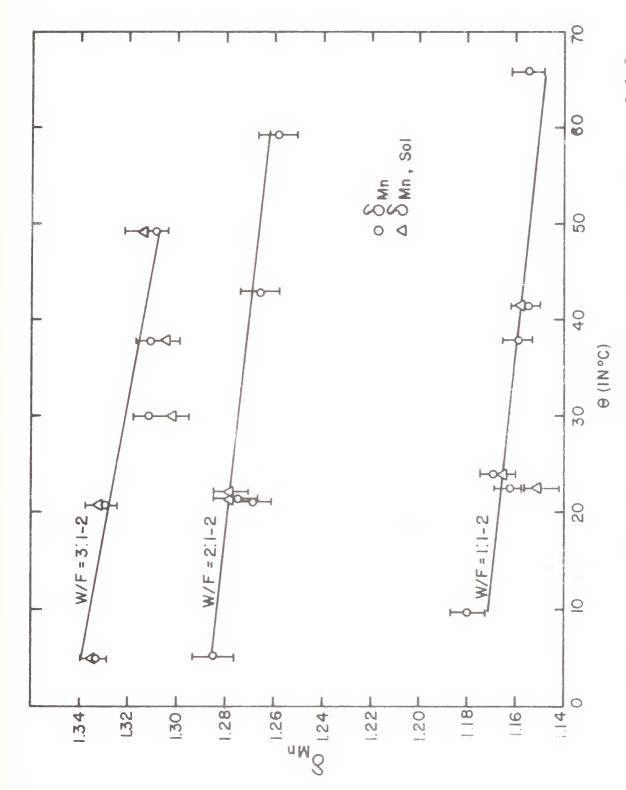


TABLE 5.3 EXPERIMENTAL DISADVANTAGE FACTORS

W/F	Date	(D ₀)	$\bar{\tilde{\mathbf{o}}}_{\mathbf{D}\mathbf{y}}$	$^{\circ}$ Mn	S _{Mn} , Sol	Ng
1 . 1 . 2	3/ 6/64 3/10/64 4/ 8/64 3/19/64 4/ 7/64 3/11/64	9.66 22.50 23.48 38.00 41.46 65.93	1.156±0.009 1.172±0.009 1.172±0.009	1,180±0.006 1,163±0.006 1,169±0.006 1,159±0.006 1,156±0.006	1,151±0,008 1,167±0,007 1,158±0,007	1.193±0.010 1.182±0.010 1.177±0.010
2.1-2	5/19/64 5/13/64 5/15/64 5/14/64 5/12/64 5/26/64	5.12 21.5 42.95 59.25 22.1 21.4	1.288±0.010	1,285±0,008 1,275±0,008 1,266±0,009 1,259±0,008	1,278±0.007	1,265±0,010 1,284±0,010 1,271±0,010
3:1-2	7/13/64 7/7/64 7/18/64 7/17/64 7/16/64	4.92 20.7 30.0 37.82 49.3	1,380±0,005 1,374±0,005 1,341±0,006 1,343±0,006 1,353±0,007	1,334±0,005 1,330±0,005 1,312±0,006 1,311±0,005 1,309±0,006	1,334±0,006 1,332±0,006 1,302±0,007 1,305±0,006 1,313±0,009	1,340±0,008 1,357±0,007 1,299±0,008 1,326±0,008 1,308±0,007

TABLE 5.4

	CORRECTION FACTOR TO	N FACTOR	TO Sexp	FOR MISS	FOR MISSING PART OF MODERATOR FOIL	OF MODE	MATOR FO	II	
	Dy	1;1 Mn		Dy	2:1 Mn		Dy	3:1 Mn	Λ
$V^{\rm m}/V^{\rm f}$		1.0122			2.0174			3.0111	
$v_{\rm foil}^{\rm f}/v_{\rm foil}^{\rm m}$	1.04615	1.04615 1.0758	1.05136	1.05136 0.52099	0.51260	0.50916	0.34571	0.51260 0.50916 0.34571 0.34466 0.34202	0.34202
$R = \frac{v^m v_{foil}^f}{v^f v_{foil}^m}$	1.0589	1.0889	1.0642	1.0510	1.0341	1.0272	1.0410	1.0378	1.0300
⁵ clad		1.14087			1.15325			1.15677	
1+5-1 (R-1) R	0.993	0.980	0.992	0.994	966.0	966.0	0.995	0.995	966.0



Manganese Disadvantage Factors vs Temperature; 3:1-2. Figure 5.6:

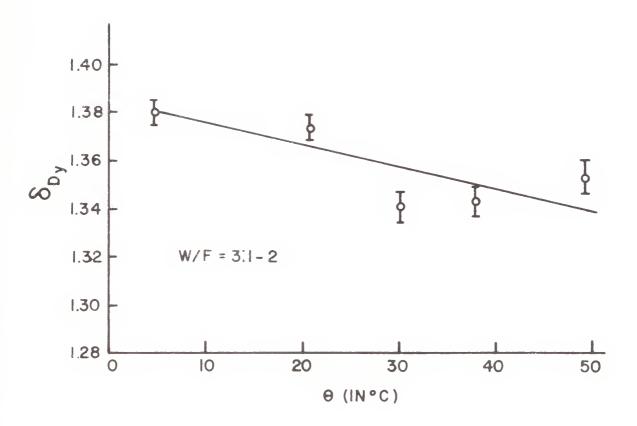


Figure 5.7: Dysprosium Disadvantage Factors vs Temperature; 3:1-2.

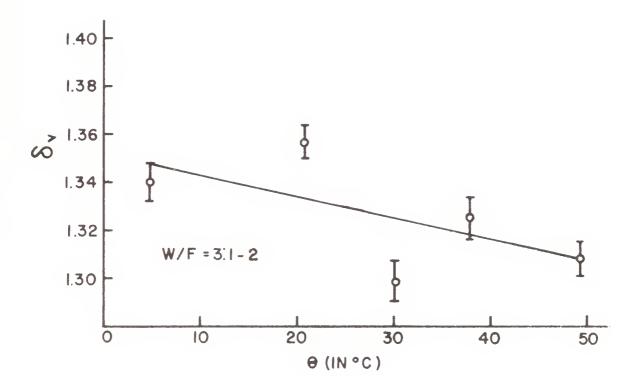


Figure 5.8: Vanadium Disadvantage Factors vs Temperature; 3:1-2.

5.6 DISCUSSION OF RESULTS

5.6.1 Foil Construction and Positioning Errors

Moderator foils were punched from stock using a machined die of appropriate shape. The radius of the circular cuts taken in the corners of the triangles was that of a standard drill size (0.6875 inch) rather than the exact radius of the outside of the fuel rods (0.666 inch). This gave all the moderator foils a slightly smaller volume than the actual moderator volume of interest.

An estimate of the error associated with inexactly cut foils can be made as follows. First it is assumed that the foil thickness is uniform. A second assumption is that the only error in foil construction will be in making the moderator foil. This is justified somewhat in that the fuel foil is made from a die with less than 0.5% tolerance. The following equation is written for the correct experimental disadvantage factor for a foil with 1/v absorption cross section:

$$\delta_{\text{correct}} = \frac{\overline{C}^{\text{m}}}{\overline{C}^{\text{f}}} = \frac{(\overline{N}_{\text{foil}}^{\text{m}} V_{\text{foil}}^{\text{m}} + \overline{N}_{\text{nf}}^{\text{m}} V_{\text{nf}}^{\text{m}})/V^{\text{m}}}{(\overline{N}_{\text{foil}}^{\text{f}} V_{\text{foil}}^{\text{f}})/V^{\text{f}}}, \quad (5.1)$$

where the subscript "foil" indicates a property of the foil, and the subscript of indicates a property of the missing portion of the foil, or the "non-foil." All other symbols have been previously defined. The second assumption above

sets $V^f = V^f_{foil}$ Equation (5 1) can then be rewritten as

$$\delta_{\text{correct}} = \delta_{\text{meas}} \left[(V_{\text{foil}}^{\text{m}}/V_{\text{m}}^{\text{m}}) + (\overline{N}_{\text{nf}}^{\text{m}}V_{\text{nf}}^{\text{m}}/\overline{N}_{\text{foil}}^{\text{m}}V_{\text{m}}^{\text{m}} \right]$$
 (5.2)

where $^{\circ}_{meas}$ is the previously reported disadvantage factor as given in Table 5.3. Assuming that the missing section of the foil is from the circular region near the fuel cladding, the neutron density cladding disadvantage factors of MacVean can be used to approximate $\overline{N}_{nf}^{m}/\overline{N}_{foil}^{m}$. This will result in an overestimate of the correction factor. Let

$$R = V^{m}/V_{foil}^{m}$$
 (5.3)

Then, Eq. (5.2) becomes

$$\delta_{\text{correct - meas}} R^{-1}[1+(R-1)/\delta_{c}]$$
 (5.4)

where $\delta_{\mathbf{c}}$ is the cladding disadvantage factor

Typical values of $V_{\rm foil}^{\rm f}/V_{\rm foil}^{\rm m}$ were taken from foils used in the experiments. Table 5 5 gives the values of the corrections for the three foils and three water-to-fuel ratios used. It can be seen that the correction is small, and generally within the accuracy of the experiment. Because it is a small correction, and because it is not an accurately determined correction, it has not been applied to the experimentally measured disadvantage factors

 $[\]frac{43}{}$ C. R MacVean, footnote 2, p. 141

TABLE 5.5

COMPARISON OF THEORY AND EXPERIMENT -- DISADVANTAGE FACTORS

M/F		~ ° °		2:1		3.1	
Foil	$_{\delta}$ $a/$ (at 20° C)		Scalc Sexp Scalc		Scalc Sexp Scalc		calc exp
Dy	<pre>bexp calc,1/v calc</pre>	1.162±0.011 1.256 1.269	0.075	1.287±0.010 1.355 1.371	0.050	1,366±0,005 1,424 1,446	0.041
М	<pre>bexp bexp, sol calc/1/v calc</pre>	1.167±0.005 1.165±0.007 1.209 1.208	0.036	1.279±0.007 1.278±0.007 1.314 1.310	0.027	1.324±0.004 1.332±0.006 1.387 1.386	0.045
>	bexp calc,1/v calc	1.189±0.011 1.238 1.241	0.041	1.284±0.010 1.341 1.340	0.042	1.335±0.007 1.414 1.414	0.042

S VS O.

 $\frac{b}{c}/d\theta$ was determined by least squares fitting of $\frac{c}{c}/$ See Table 4.4.

Table 5.5 continued

(10-4/°C)	(10 4/°C)			
Dy	dop/de		1	-9 , 0±1 , 7
Mn	ep/ ^{uW} gp	-3.9±1.4	-4,4±1,9	-7 .0±1 ,2
\triangleright	$\theta p/\Lambda g p$	-2.8+2.5	1	-9°2±2°2
Theo- retical Calcu- lation	/2 6p/ugp -	-3.46	-6,02	-7.91

Errors resulting from improper vertical positioning of the moderator foils in the experimental assembly are expected to be negligible. The flux change in the axial direction at the foil position in the unit cell is of the order of one or two per cent per inch. Positioning accuracy is estimated to be about 0.1 inch. The resulting error is then seen to be about 0.2% in count rate.

A small error may be introduced by the presence of the lucite support plate for the moderator foil. This plate is one-eighth-inch thick and of approximately the same shape as the moderator foils. It is suggested that further experimental work be done with different thicknesses of lucite to investigate the magnitude of this effect.

The error associated with the finite thickness of the foils has not been investigated experimentally. It was assumed in Chapter 4 that the self-shielding factors for the fuel and moderator foils were equal. In conjunction with the investigation of lucite thickness effect, it is suggested that the disadvantage factor be measured as a function of detector foil thickness.

The process of dissolving the foils for the "soluble" disadvantage factor measurement is not expected to contribute any error to the measurement. The chemical handling technique employed standard volumetric flasks and volumetric pipettes. The pipettes are estimated to be accurate to about 0.25% and the flasks to about 0.1%. The error should

be uniform for each aliquot, and therefore cancel from the ratio which is the disadvantage factor.

Weighing of the foils was accurate to 0.1 mg which represents a maximum error of less than 0.3% for moderator foils of the 1:1 core. For all other foils the error is less than 0.2%.

5.6.2 Foil Induced Flux Perturbations

There are two perturbations associated with inserting foils into the reactor for measurement. One effect is the depression of the flux by the foil itself as in the case of an absorber being placed into the low absorption region of the moderator. This would tend to reduce the measured value of the flux in the moderator. This effect could be determined by measuring the foil activity per unit weight as a function of foil thickness and extrapolating to zero foil thickness.

The second effect is present in the fuel foil. Here, a highly absorbing region is replaced by a lightly absorbing foil. Neutrons may stream into the foil and the average flux in the foil would then be higher than that in a corresponding fuel region. This effect could also be determined by extrapolation to zero thickness foils.

Both of these effects tend to make the measured disadvantage factor lower than the ratio of the neutron densities appropriate to the two regions under investigation.

An estimate of the first correction, called the outer flux perturbation, was made using the procedure outlined in ANL $5800.\frac{44}{}$ A correction factor, defined as the ratio of the activation in the perturbed flux to activation in the unperturbed flux was calculated for the three foil materials and for water-to-fuel ratios of 1:1 and 3:1 using the approximations given to the transport theory calculations of Ritchie and Eldridge. This correction is for a coin shaped foil, but the moderator foils used here were of the shape shown in Figure 5.3. An equivalent radius for these foils was taken to be 0.5 cm and 1.0 cm for the 1:1 and 3:1 cores respectively. The correction was then estimated to be: 0.3-0.8% for dysprosium, 0.6-1.6% for manganese, and 0.1-0.4% for vanadium where the lower values are for the 1:1 core. The correction increases the measured disadvantage factors by this amount.

Because of the smallness of the corrections, and the uncertainty in their accuracy, they have not been applied to the measured disadvantage factors. It is recommended, rather, that an attempt be made to measure them experimentally.

 $[\]frac{44}{}$ L. J. Templin, footnote 24, p. 670.

5.6.3 Flux Perturbations Due to the Activation Rods

Axial flux scans taken on the 1:1 core showed a large flux peaking near the ends of the fueled section of the activation rods. This peak is a result of replacing the fuel region of a normal fuel rod with the aluminum support pieces of the activation rod. Peaking was most pronounced in the 1:1 core because of undermoderation for this water-to-fuel ratio. The peaking may have been sufficient to affect the vanadium and possibly the dysprosium disadvantage factors in the 1:1 core. The manganese disadvantage factors are not expected to be influenced by this peaking because these foils were in the center of the fueled section of the activation rod.

Peaking was less pronounced in the 2:1 and 3:1 cores. In addition, the fueled section of the activation rods was lowered in successive runs as indicated in Figure 5.1. The first change was made so that the vanadium foils were in the center of the core. This was changed again to the "symmetric" activation rod wherein the center of the fueled section of the activation rod is at the center of the fuel region of the core.

The effect of the peaking may result in some inaccuracy in the measured value of the disadvantage factors for vanadium and possibly dysprosium, but the temperature dependence of the disadvantage factors should not be affected.

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The only way to remove this effect is to resume use of the full length decappable fuel rods. A minimization of the effect can be achieved by using only one set of foils and placing them at the center of the fueled region of the activation rod.

5.6.4 Comparison of Experiment and Theory

Table 5.5 compares theory and experiment and shows that (1) dysprosium disadvantage factors lie between 4 and 8% lower than theory, (2) manganese disadvantage factors lie between 2.4 and 4.5% lower than theory, and (3) vanadium disadvantage factors lie about 4% lower than theory. However, all measured values of the temperature dependence of the disadvantage factors agree with the theoretical values within the limits of experimental error.

5.7 CONCLUSIONS

The disadvantage factor was measured for three water-to-fuel ratios using foils of three different materials. Values of the measured disadvantage factors are consistently a few per cent lower than the calculated values. Further refinements in the experimental technique, specifically utilization of different thickness foils and moderator support plates, could reasonably be expected to bring the experimental values of the disadvantage factor into closer agreement with the calculated values.

The temperature dependence of the disadvantage factor was measured for three water-to-fuel ratios. Measured values of the temperature dependence agree within experimental errors with the theoretical values as calculated by MacVean. $\frac{45}{}$

 $[\]frac{45}{}$ C. R. MacVean, footnote 2, p. 143

CHAPTER 6

SUMMARY AND CONCLUSIONS

6.1 ISOTHERMAL TEMPERATURE COEFFICIENT OF REACTIVITY

6.1.1 Summary

The isothermal temperature coefficient α is defined as d ρ /d θ where ρ is reactivity and θ is the temperature of all parts of the core. The isothermal temperature coefficient was measured by differencing, at a series of closely spaced values of θ , values of ρ computed from observed clean-core periods using a local code RHOFIT. Temperatures were determined by averaging readings from four thermocouples distributed through the moderator; auxiliary tests showed the temperature could be made uniform within $\pm 0.1^{\circ}\text{C}$.

A preliminary calculation of α was carried out using two group, two region, first order perturbation theory as outlined by Larrimore. 46/ A computer program calculated the fluxes and adjoint fluxes and used them in the standard perturbation theory reactivity equations to find the isothermal temperature coefficient. Dependence of α on temperature can be ascribed to two contributions: a rapidly varying one proportional to the volumetric coefficient of thermal expansion of water,

^{45/} W. E. Schilling and D. H. Bryce, private communication (March, 1964).

Sec. 6.1

and a second one, nearly constant over the investigated temperature range, which is due to temperature dependence of microscopic cross sections and other small temperature dependent effects. These considerations lead to an equation for α of the form

$$\alpha = A + B \beta_{H_2O} , \qquad (6.1)$$

where $\beta_{H_{\underline{2}}0}$ is the volumetric coefficient of thermal expansion for water.

Experimental temperature coefficients were determined for nominal water-to-fuel ratios of 1:1, 2:1, 3:1, and 4:1. Statistical errors in values of α are generally less than 10%. For the cores studied, and over the temperature ranges used (1:1, 5-70°C; 2:1, 5-78°C; 3:1, 5-62°C; 4:1, 7-45°C), the isothermal temperature coefficient is well represented by Eq. (6.1) where A and B are different constants for each core. A comparison of theoretical values of A and B with experimental values found from a least-squares fit to Eq. (6.1) shows a need for more sophisticated calculations to obtain better agreement with experiment.

6.1.2 Conclusions

Temperature dependent excess reactivities for various fuel loadings were determined for four water-to-fuel ratios

 $[\]frac{46}{}$ J. A. Larrimore, footnote 14, pp. 185-210.

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of the Cornell University Zero Power Reactor with sufficient accuracy to allow planning of further temperature dependence studies.

The isothermal temperature coefficient of reactivity was measured for four water-to-fuel ratios with an accuracy which is comparable to that previously reported in the literature. The predicted and verified linear dependence of α on $\overline{\beta}_{H_2O}$ had not been reported previously.

Since the experimental results are based on period measurements on a clean core, and since the calculations were done with a simple two group model, the disagreement between calculated and measured values of A and B indicates the need for a refinement in the calculations.

6.2 TEMPERATURE DEPENDENCE OF THERMAL DISADVANTAGE FACTORS6.2.1 Summary

The neutron density disadvantage factor δ_n and the experimentally measured disadvantage factor δ_{exp} are defined by the ratios $\delta_n = \overline{N}^m/\overline{N}^f$ and $\delta_{exp} = \overline{C}^m/\overline{C}^f$ where \overline{N} and \overline{C} are respectively the spatially averaged neutron density and foil count rate per unit volume; superscripts m and f indicate respectively the moderator and fuel regions of the reactor.

MacVean's calculation of thermal lattice parameters $\frac{47}{}$ gives the temperature dependence of the disadvantage factor.

 $[\]frac{47}{}$ C. R. MacVean, footnote 2, p. 143.



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Since the calculated changes are small, highly accurate experiments were required for comparison. Experimental disadvantage factors were measured for three water-to-fuel ratios over the temperature range 5-65°C.

An integral foil counting method was used employing a 0.600±0.001-inch diameter foil in the fuel and an appropriately shaped moderator foil. Five-mil thick foils of dysprosium (5.24% dysprosium in aluminum), manganese (P-metal), and vanadium were chosen because their cross sections are nearly 1/v. Two counting methods were used. One was to dissolve the manganese foils in nitric acid and gamma-count aliquots of the solutions in a well-type scintillation counter. The other method was to beta-count solid foils in a proportional flow counter. Results of the two methods agree within statistical errors.

Experimental disadvantage factors were least-squares fitted to linear functions of temperature. Agreement between theory and experiment for the temperature dependence of the disadvantage factors is within the experimental error for all cores and foils, but the disadvantage factors themselves are a few per cent lower than the calculated disadvantage factors -- a result also found in the Brook-haven and Westinghouse work reported by Honeck. 48/

 $[\]frac{48}{}$ H. C. Honeck, footnote 10, p. 49.

Sec. 6.2

6.2.2 Conclusions

Experimental determination of the thermal disadvantage factor was accomplished quite accurately using the technique of dissolving the foils and gamma-counting aliquots of the solutions. Beta-counting of the solid foils gave satisfactory results providing that measured values were corrected for the different geometrical counting efficiencies of different shapes of foils. The error for both methods was less than one per cent, an improvement on previously reported measurements.

Theory and experiment disagree by a few per cent on the value of the disadvantage factor. This has been a common result, as mentioned above. Several factors may contribute to this disagreement: (1) flux perturbations due to finite thickness foils, (2) flux perturbations due to the lucite moderator foil support plate, (3) flux perturbations due to the use of activation rods with a shorter fuel region than normal fuel rods, (4) inexactly shaped moderator foils, and (5) a small error in the calculation of the disadvantage factor. The first two possibilities could be studied by using different thicknesses of foils and of moderator foil support plates. The third could be eliminated by using full length decappable rods, or minimized by placing foils only at the center of the fueled section of the activation rod. A more expensive die could

be made for punching the moderator foils to eliminate the fourth error source. Further study could be made on the calculational techniques for the disadvantage factor; however the estimated accuracy of 2% for the calculated values of the neutron density disadvantage factors by MacVean $\frac{49}{}$ indicate that the calculations probably would not change much with slight refinements to the code.

Agreement between theory and experiment for the temperature dependence of the disadvantage factor is within the experimental error; however the experimental error in these results varies from about 20% to about 90% because small differences were taken between relatively large numbers to obtain the temperature dependence.

6.3 PROPOSALS FOR FURTHER STUDY

When the perturbation theory calculations of the temperature coefficient are brought into agreement with the experiments, these same calculational techniques can be used to predict the effect of adding soluble poisons to the moderator. It would then be of interest to measure the temperature coefficient of reactivity as a function of the distributed poisons.

As indicated earlier, it would be of great interest to investigate the effect that changing the foil thick-

^{49/} C. R. MacVean, footnote 2, p. 111.



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nesses would have on the disadvantage factor measurements. It might be of further interest to investigate the disadvantage factor, and possibly its temperature variation, using resonance foils to study different energy regions.

In conjunction with the above proposals, it would also be interesting to vary the thickness of the lucite moderator foil support plate and determine its effect on the measured value of the disadvantage factor. Another study could be made using polyethylene support plates.

Further into the future, it might be of interest to measure these same parameters on cores which have different geometrical shapes. For example a square or long, thin lattice could be set up instead of a cylinder. The ability to properly predict the temperature coefficient for these geometries would be a measure of the accuracy of calculating the reflector contribution to the isothermal temperature coefficient of reactivity.

APPENDIX A

LATTICE PARAMETERS FOR THE CORNELL UNIVERSITY ZERO POWER REACTOR

Fuel Material	Uranium Dioxide
Fuel Rod Diameter, in:	0.600±0.003
Fuel Density, gm/cc:	10.381±0.52%
Fuel Enrichment, Weight Percent U ²³⁵ :	2.070±0.10
Fuel Enrichment, Atom Percent U ²³⁵ :	2.096±0.90
Oxygen to Uranium Number Ratio:	2.01:1
Fuel Molecular Weight:	270.26(physical)
Cladding Material:	6061-76 aluminum
Cladding Density, gm/cc:	2.70
Cladding Inner Diameter, in:	0.610±0.002
Cladding Thickness, in:	0.028±0.003
Fuel Element Diameter, in:	0.666±.006

 $[\]underline{a}$ / S. S. Berg, see footnote 1.

CORNELL UNIVERSITY ZERO POWER REACTOR LATTICE PARAMETERS

		Nominal W	Water/Oxide Volume	Volume Ratio	10
	1:1	1.5:1	2:1	3:1	4:1
Lattice Pitch, in.a/	0,8560	0.9470	1.0300	1.1770	1,3090
Equivalent Cell Radius, cm.	1,1416	1,2629	1.3736	1,5696	1.7457
Fuel Element Radius, cm.	0.8458	0,8458	0.8458	0.8458	0,8458
Fuel Rod Radius, cm.	0.7620	0.7620	0.7620	0.7620	0.7620
Water Area, cm^2 .	1.8465	2.7632	3,6800	5.4927	7,3261
Cladding Area, cm ² .	0.3621	0.3621	0.3621	0.3621	0.3621
Fuel Rod Area, cm ² .	1.8242	1.8242	1.8242	1.8242	1 8242
Actual Water/Oxide Volume Ratio.	1,0122:1	1,5148;1	2.0174:1	3.0111:1	4,0162;1
a/ D. D. Clark, "The Cornell University Nuclear Reactor Laboratory," CURL-1, Cornell University (1961)	University L)	Nuclear R	eactor Labo	ratory," C	.URL-1,

APPENDIX B

ISOTHERMAL TEMPERATURE COEFFICIENT DATA REDUCTION

Tables B.1 - B.4 give the following information in tabular form: date of the experiment, reference run number, number of fuel rods N, temperature θ in °C, period T in seconds, excess reactivity $\rho_{\rm excess}$, reference numbers of the two runs used to calculate $\Delta\rho/\Delta\theta$, $\Delta\rho$, $\Delta\theta$, $\Delta\rho/\Delta\theta$ = α , the average temperature for the two runs $\overline{\theta}$, and the volumetric coefficient of thermal expansion of water at the average temperature $\overline{\theta}_{H_20}$. Figure B.1 is a curve of β_{H_20} vs θ obtained by differencing values of relative volume given in the $\underline{\text{Handbook of Physics and}}$ Chemistry. $\underline{50}/$

 $[\]frac{50}{}$ C. D. Hodgman, footnote 27, p. 2143.

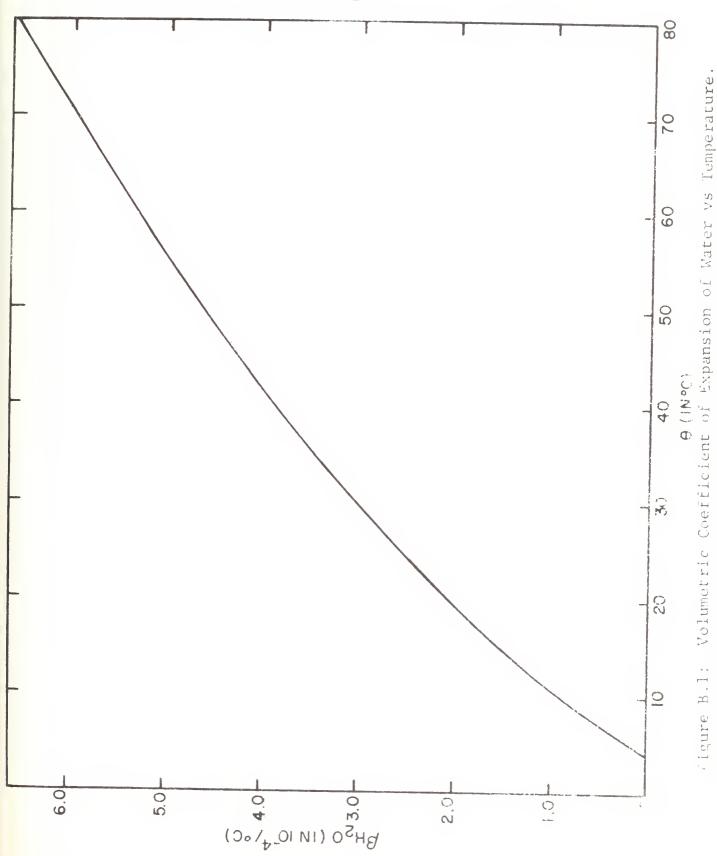


TABLE B.1 ISOTHERMAL TEMPERATURE COEFFICIENT DATA REDUCTION

					1	:1-2					
Date	71.72	Z	θ	I	Pexcess	Runs Used	ΔĮ	97	90/√0	Ю	la la
7		Rods	၁့	sec		^	→	o.	D°/⊅	O.	10-4°C-1
/18/	-	5	2.7	2.8±1.	1 18.56±0.2		1			:	-
2/18/64	2	457	27.18	54.0±0.4	4 15.92±0.08	1,2	9.	4.	0.0±09.	4.9	5
/18/	4	5	1.4	$0.9\pm0.$	11.94±0.0		3	4.28	0.93±0	29.32	2.96
/18/	2	2	1.2	$3.0\pm0.$	21.80 ± 0.1	-	- i	- 1	-	1	1
/20/	9	\sim	7.2	4.2±0.	14.12±0.0		7	6.02	.28±0.0	4.2	3.42
/20/	7	2	0.9	529±63	0.87 ± 0.3	1	. 2	7.	1.51 ± 0	41.61	4.02
/20/	∞	9	5.6	38.0 ± 0 .	19.98±0.1	-	-1	1	1	1	-
/20/		9	1.5	$6.8\pm0.$	0.0∓99.6	8,9	-10.32	5.82	-1.77 ± 0.03	48.59	4.53
/20/		9	6.6	$25.8\pm0.$	25.17±0.2	. 1	1	- 1	1	- 1	1
/20/		9	9.6	47.7±1.	7.45±0.0	10,11	-17.72		-1.84 ± 0.03	54.79	4.98
/20/		9	8.9	$36.3\pm0.$	20.56 ± 0.1	- 1	ı	- 1	ı	-	1
/20/	$\stackrel{\circ}{\sim}$	95	4.8	38.6±2.	7.87±0.1	2,13.	12.7	6.	2.15±0.0		4.
/20/	3	9	4.8	$35.6\pm3.$	7.98±0.1	12,13.2	-12.58	5.91	-2.13 ± 0.03	61.94	5.45
/20/		$\overline{}$	2.7	$28.1\pm0.$	23.97±0.1	1		- 1	ı	- 1	1
/20/		$\overline{}$	9.8	07.1 ± 0 .	0.0∓49.6	14,15	-14.33	7.17	-2.00 ± 0.03	66.28	5.72
/9 /		\sim	4.8	48.7±0.	17.04±0.2	. 1	-1		- 1	1	1
/9 /			8.3	8.6±0.	17.07 ± 0.2		I		1	1	1
19 /		5	9.	$0.7\pm1.$	11.96 ± 0.1		1	1	;	1	1
/13/	∞	45	5.5	0.4±0.	16.67±0.1	7,1	7.0	2.8	.14±0.0	6.	4.
/13/		5	5.7	6.0 ± 0.8	15.52 ± 0.1		- 1.55	+7.34	-0.21±0.02	2	1.17
/24/			3.0	4.3±0.	18.14±0.2	2,2	2.2	4.0	.54±0.0	5.1	.5
/24/		5	3.0	$6.0\pm1.$	11.40 ± 0.1	,2	4.1	7.3	.56±0.0	.3	6.
/25/		5	7.0	3.0±0.	14.30±0.1	\ I	1	- 1	1	1	1
/25/	26	5	\vdash	9.4±0.	19.55 ± 0.1	25,26	+ 5.25	-4.90	-1.07 ± 0.03	34.62	3.45
/25/		5	1.9	8.7±1.	10.27 ± 0.0	. 1	1	- 1	1	1	1
16 /		\sim	9.8	8.2±0.	23.93±0.3	6,3	9.8	7.3	.33±0.0	3.5	.3
						31,25	+ 9.63	-7.21	0	33.46	3.34
						1,2	4.3	2.3	1.90 ± 0.0	1.0	1
						8,1	1.1	0.2	0.11 ± 0.0	9.0	6.

TABLE B.2

ISOTHERMAL TEMPERATURE COEFFICIENT DATA REDUCTION

	10.	°C 10-4°C-1						.48 3.1	6.64 3.62		.63 4,1	9.88 4.62		5.16 5.00		,25 5,2	4.71 5.62		9,51 5,92		3,61 6,20		.83 0.3	.50 0.7	.01 1,2	8.11 1.85	.59 2.4	.32 2.8	
	97/dQ	\$/°C						0,61±0,04 3	0±0.04 3		0.94±0.04 4	$-1,22\pm0.03$ 4		-1,36±0,05 5		1,30±0,07 5	-1.52 ± 0.03 6		-1,60±0,04 6		-1.73±0.04 7		.43±0.19	.32±0.04	.02±0.04 1	-0.10±0.04	.37±0.04 2	.54±0.02 2	
	$\Theta \nabla$	J.						4.98	+5.32		8.26	+6.24		+4.68		87	4.98		+7.87		+8.59		06.	.45	.57	+5.62	.34	1	
	S Ap	g						3,0	-4.26		7.7	-7.59		0 -6.35		\sim	-7.5		5 -12,56		7 -14.86		+0.3	+1,4	0.0	2 -0.55	-1,9	-2.2	
-2	Run	Use						-	4,5		\sim	7		9,1		11,1	2		14,1		16,1		8,1	9,2	0,2	\sim	2,2	3,2	
2:1	Pexcess	ĺ	1.95±0.1	21.58±0.22	1.67 ± 0.3	1.63±0.3	$1,60\pm0.3$	8.52 ± 0.2	4.26±0.1	4.52±0.3	6.73±0.2	9.14±0.0	8.84±0.2	2.49 ± 0.1	4.01±0.3	6.39±0.1	8.84±0.0	1.78 ± 0.2	9,22±0.0	5.98±0.3	1.12±0.0	3.12 ± 0.1	3.51±0.1	4,92±0.1	5.01±0.1	4.46±0.1	2.47±0.1	0.25±0.0	
		sec	5,6±0.	$31,5\pm0.5$	1,3±0,	1,4±0,	$1,4\pm0$	$0.2\pm 0.$	9,2±0,	5.4±0.	6.9±0°	7.2±1.	39.2±0.	1.2±1.	$6.3\pm0.$	8,4±0.	1,9±1,	$1,0\pm0$	6.0±1.	2,9±0,	3,3±0,	6,6±0.	3.9±0.	5.5±0.	$5,1\pm0.$	8,1±0.	1,4±1.	2.6±1.	
	0	o.	9,2	29.00	0,6	∞ °,	8	3,9	9,3	8.5	6.7	3.0	2 ,8	7 ,5	6.3	2.2	7:2	5.5	3.4	9.3	7.9	5.3	6.2	0.7	5,3	0,9	6.2	0,3	
	Z		\sim	228	\sim		\sim		\sim	\sim	\sim	\sim	\sim	\sim	\sim	\sim	\Im	\sim			\sim	\sim	\sim	\sim	\sim	\sim	\sim	\sim	
	Run		2	\sim	3 ° 5	9	9		9	6,2	_	00						14											
	Date		/21/6	4/21/64	/21/64	/21/6	/21/64	/21/6	/21/6	/21/6	/21/6	/21/6	/21/6	/21/6	/21/6	/21/6	/21/6	/23/6	/23/6	/23/6	/23/6	/27/6	/27/6	/27/6	/27/6	/27/6	/27/6	/27/6	

 $\frac{a}{b}$ /One control rod at 51.00 inches. $\frac{b}{a}$ /All control rods at 51.00 inches.



TABLE B.3

ISOTHERMAL TEMPERATURE COEFFICIENT DATA REDUCTION

	147	10 °C ±					5	0	\mathcal{C}°	00	2	,	\mathcal{L}°	∞	4.27	, 7	٧.	. 2
	100 (S					3	0.2	3 , 7	8, %	2 , 3	7 . 1	3,1	7° 6	45,45	1.9	1.8	8
		D , / \$					0°∓99°	.48± ,1	0° 777°	,33±,0	17 ± 0 ,	.14±.0	00±00.	.24±.0	- 0.33±.03	,45±.0	0.45±.0	.61±.0
))					,	0.	0	Ļ	, 7	00	2	4,	6.51	4°	3	. 2
	0	O					$,10\pm,1$,52+,1	67±01	04 ± 0	0.81 ± 0.1	。69± 。1	02 ± 2	$1,32\pm,2$.2.15±.18	$2.90 \pm .1$	$2.83\pm.1$	4.45±.1
3:1-2	Runs Used						-		-	-	9	-	0,1	1,12	12,13 -	3,14.	3,14.2	4.1,15.1
	Pexcess	v	4.27±.1	.45±.8	3.58+.1	6.51+,0	$9.61\pm.0$	0.13±.09	2.80±0.1	3.84±0.1	4.65±0.1	5,34±0.1	$.36\pm0.1$	4.04±0.1	1.89	.99±0 °0	.06±0.1	.61±0.0
	\vdash	sec	9.6±0.8	4.8±5.7	$3,9\pm1.1$	63.3 ± 1.5	1.3 ± 1.2	4,7±1,1	9.3±0.8	2.3±0.8	7.0++0.7	3.8±0.7	3 ° 7 ± 0 ∘ 8	1.0±0.8	76.7±0.9	10.3±1	9.2±1	43.6±1
	① (C))	1.0	-		4.9	9°6	0.7	0,0	0.0	4.7	9,5	6.7	2.2	48.71	5.1	5.0	2.4
	Run		1	3,1	0	7	5	9	_	00					13	7	14.2	5
	Date		/10/	/10/	/10/	/13/	/14/	/14/	/14/	/14/	/14/	/14/	/15/	/15/	7/15/64	/15/	/15/	/15/

TABLE B.4

ISOTHERMAL TEMPERATURE COEFFICIENT DATA REDUCTION

	la			9						9	3.23	.2		3.93
	Ю	1			\sim	•				6.4		2.2		67.04
	θ∇/₫∇		.22±.1	22±.0	÷00+	94±.0				+1	.77±.06	6 ± 0		.70±.02
	θ∇		9.	0	6.29	4.				4.37				9.34
	QΔ		° 76±.0	$.51 \pm .1$	$6.55\pm,16$.92±.2				$3.62 \pm .27$.61±.	$\cdot 21\pm$		6.58±.19
4:1-2	Runs		•	^	3,4			7,8		9,10		0,1		3, 1
	Pexcess	26±.	.02±.0	,53±.0	30.8±.1	$1.00 \pm .2$	$1.22 \pm .2$	4.06±.1	4.05±.1	.67±.2	3.28±.4	3.88±.4	$6.80 \pm .0$	3.38±.1
	T	359.1±3.6	$84.7\pm5.$	63.4±2.	7.6±1.	3,4±0.	2.8±0.	$1.2\pm0.$	$1.2\pm1.$	3.8±0.	8.1±0.	6.9±0.	5.8±1.	5.6±1.
	Φ	6.73		9.4	5 , 7	4.1	4.2	4.1	4.2	9 .	5.9	5.9	5.00	5.1
	Z	220	\sim	\sim	\sim	\sim	\sim	\vdash	\vdash	\vdash	$\overline{}$	\vdash	\vdash	\vdash
	Run		7	\sim	7	9	7	00	6				13	
	Date	2/4/64	/ 4/	/4/	/4/	/2/	/5/	/2/	/5/	/2/	/2/	/2/	/2/	/2/



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